

Neutrino Interactions

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Intensity Frontier Department Seminar

A few words before I begin

- I view the IF department seminars as a lecture series of sorts meaning that they will be held periodically (gap of some months).
- The subject of “Neutrino Interactions” is too vast and interesting to fit into a single 45 minute discourse (just my opinion).
- I am going to start with the basics today in an effort to lay the foundation for future talks on this subject.
- I hope that each one of us here will be able to walk away with some understanding of weak interactions today. Will be helpful for future talks that detail “quasi-elastic”, “resonance”, “deep inelastic” interactions with neutrinos.

Outline

- Fundamental properties of neutrino interactions
- Types of Neutrino Interactions
 - Neutrino-Electron Scattering
 - Neutrino-Quark Scattering
 - Neutrino Quasi-Elastic Scattering
- An overview of Charged Current Quasi-Elastic Sc.
- Results from MINERvA
- Conclusions

Weak Interactions

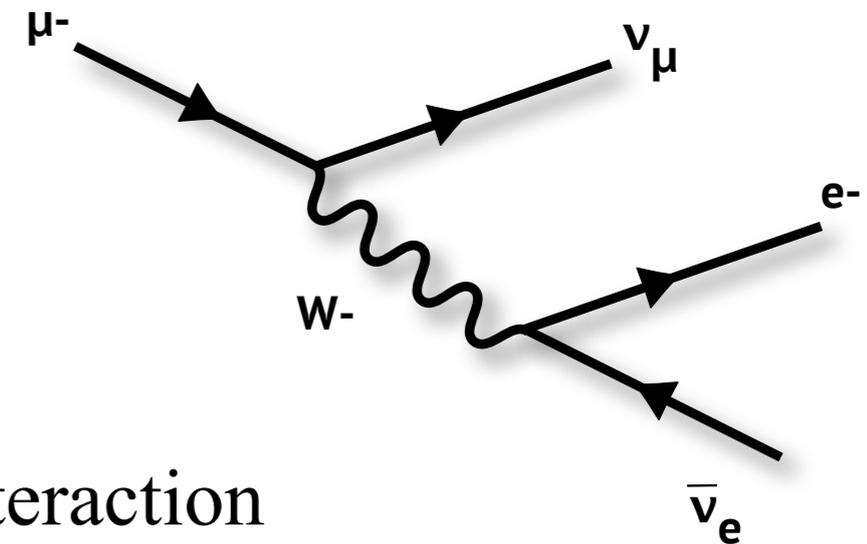
- Neutrinos are unique ! They can only interact by weak interactions !
- Colorless, electrically neutral, possess a tiny mass
- What are weak interactions ?
- Most interactions we see around us are “strong” and “electromagnetic (EM)”

Nature of Interaction	Lifetimes	Coupling Strengths
Strong	$\sim 10^{-23}$ sec	α_s
Electromagnetic	$\sim 10^{-16}$ sec	α_{EM}
Weak	$\sim 10^{-8}$ sec	α_{WEAK}

$$\alpha_{WEAK} \ll \alpha_{EM} \ll \alpha_s$$

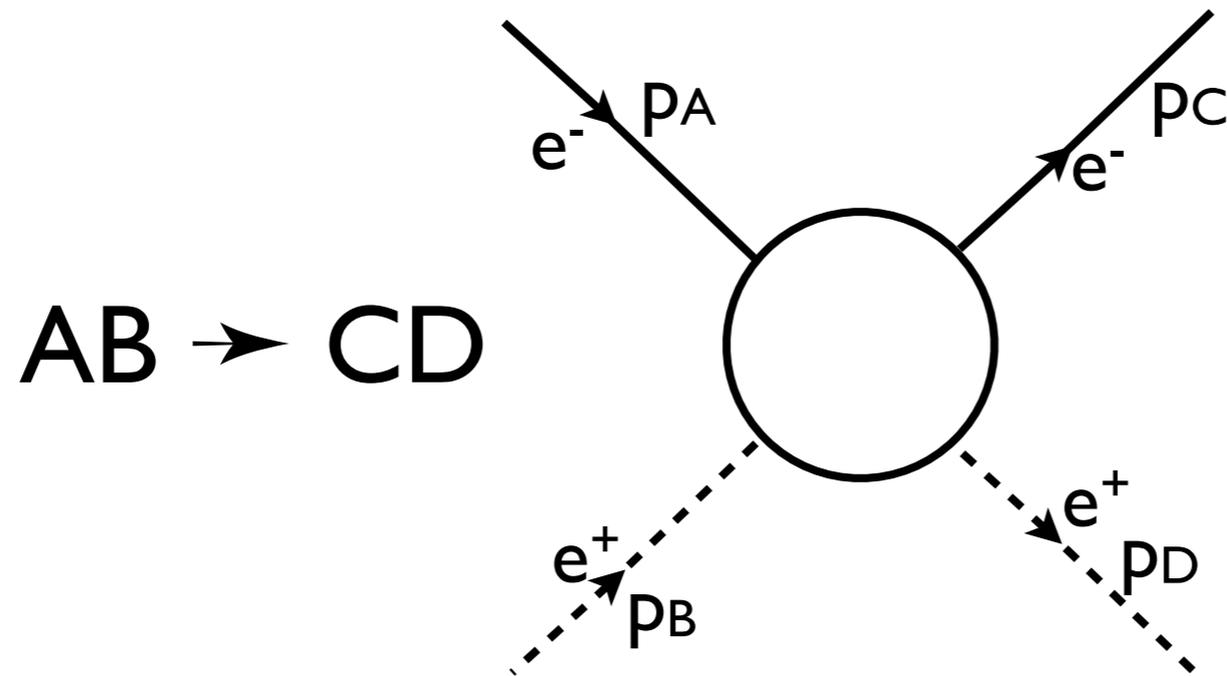
- More on why weak interactions are called “weak” later slides

Weak Interactions



- All hadrons and leptons experience this weak interaction
- However, they're often hidden by the much more rapid strong and EM interactions !
- Examples of weak interactions:
 - β -decay of atomic nuclei ($n \rightarrow p + e^- + \text{anti-}\nu_e$)
 - $\pi^- \rightarrow \mu^- \text{ anti-}\nu_\mu$ (pion is lightest charged hadron, no EM decay)
 - $\mu^- \rightarrow e^- \text{ anti-}\nu_e \nu_\mu$ (lepton number conservation)

Mandelstam variables



- Used for expressing invariant amplitude M as a function of variables invariant under Lorentz transformations

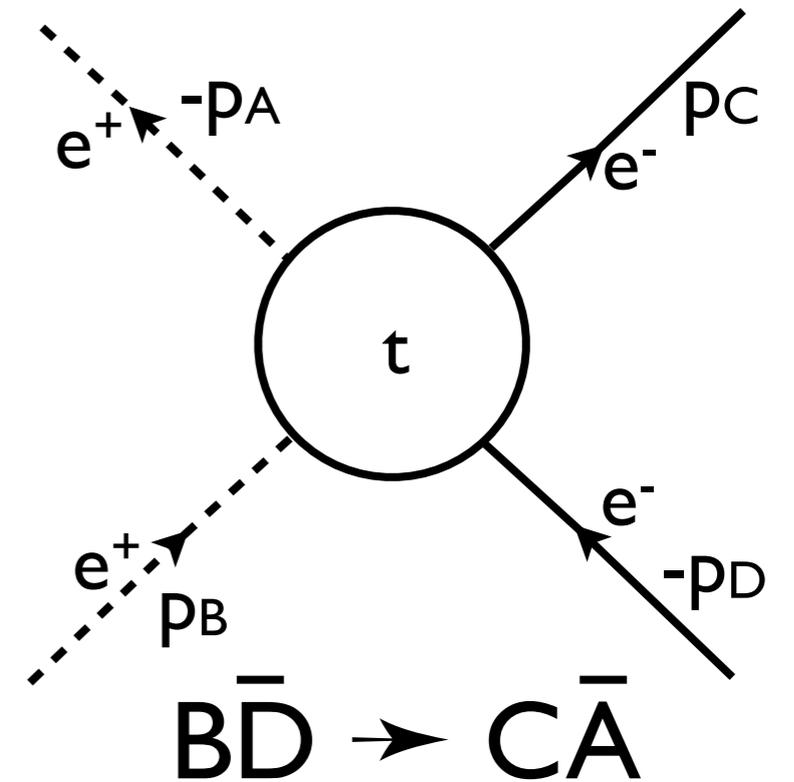
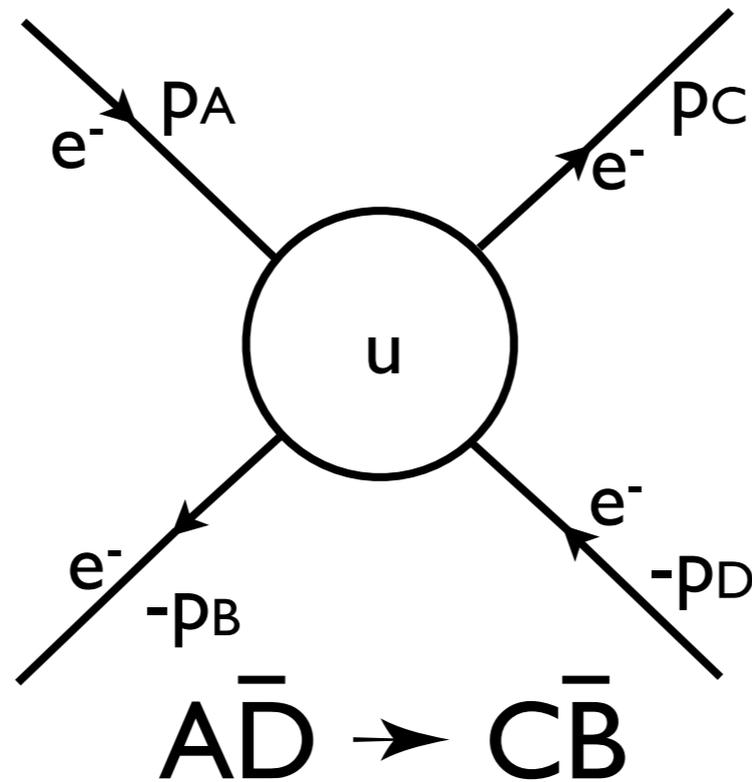
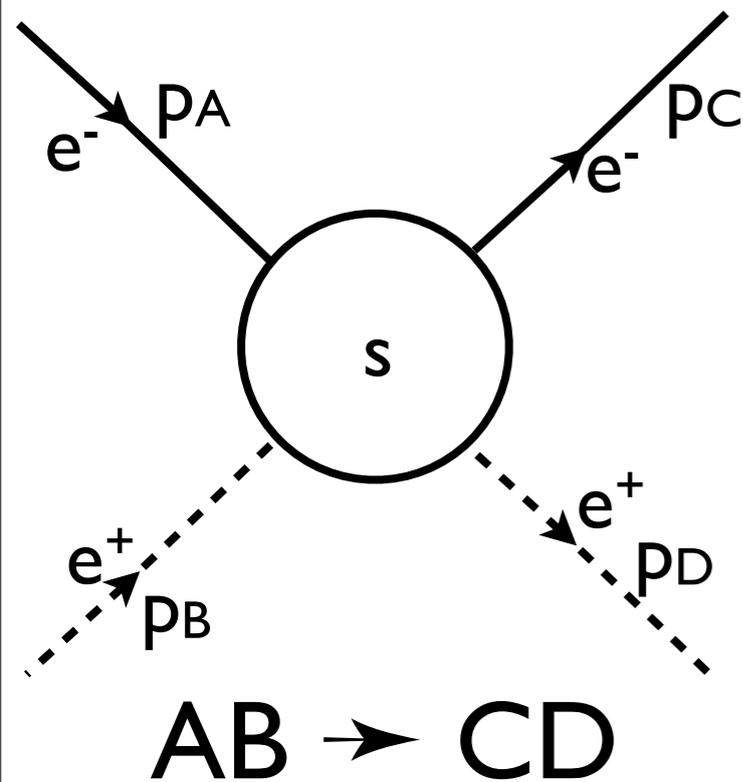
$$s = (p_A + p_B)^2$$

$$t = (p_A - p_C)^2$$

$$u = (p_A - p_D)^2$$

$$s + t + u = m_A^2 + m_B^2 + m_C^2 + m_D^2$$

Mandelstam variables (contd.)



$$s = 4(k^2 + m^2)$$

$$t = -2k^2(1 - \cos\theta)$$

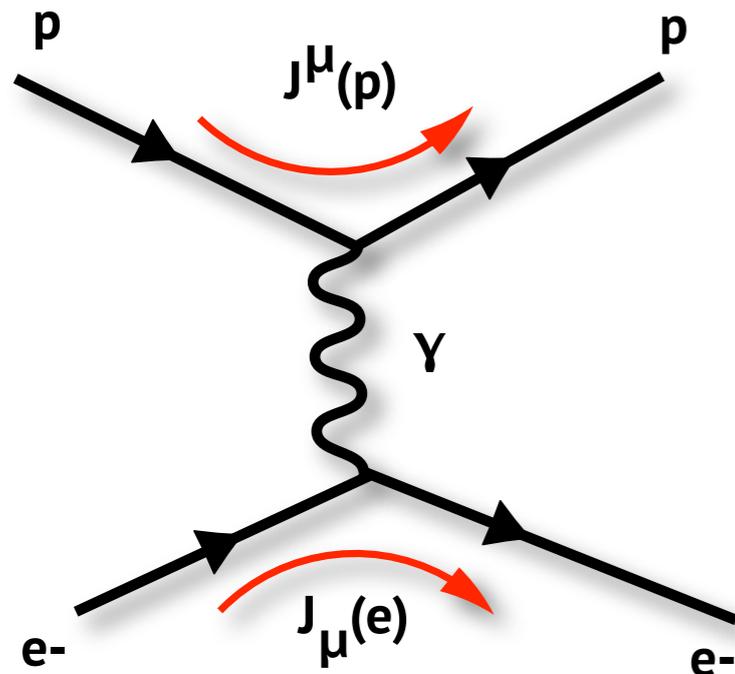
$$u = -2k^2(1 + \cos\theta)$$

- Here θ is the center-of-mass scattering angle and $k = |\mathbf{k}_i| = |\mathbf{k}_f|$
- \mathbf{k}_i and \mathbf{k}_f are momenta of the incident and scattered electrons in CM frame

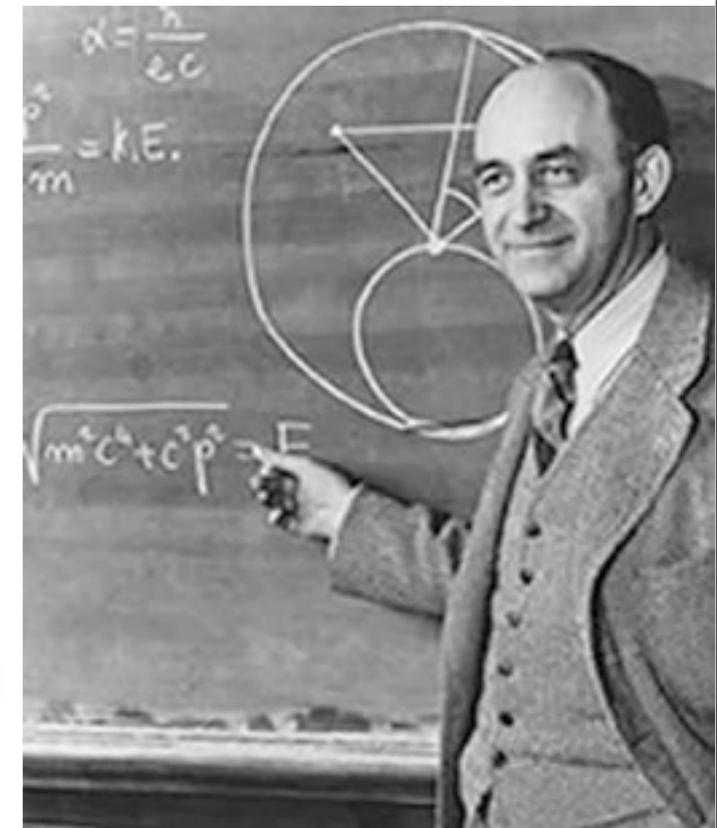
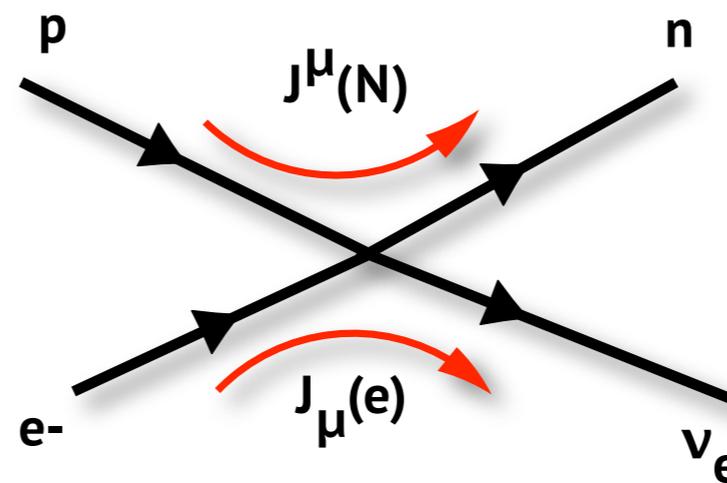
Form of the Weak Current

First Attempt: Enrico Fermi, 1932

Electron-proton (EM) scattering



β -decay (Weak) process



$$M_{em} = (e\bar{u}_p\gamma^\mu u_p) \left(\frac{-1}{q^2} \right) (-e\bar{u}_e\gamma^\mu u_e)$$

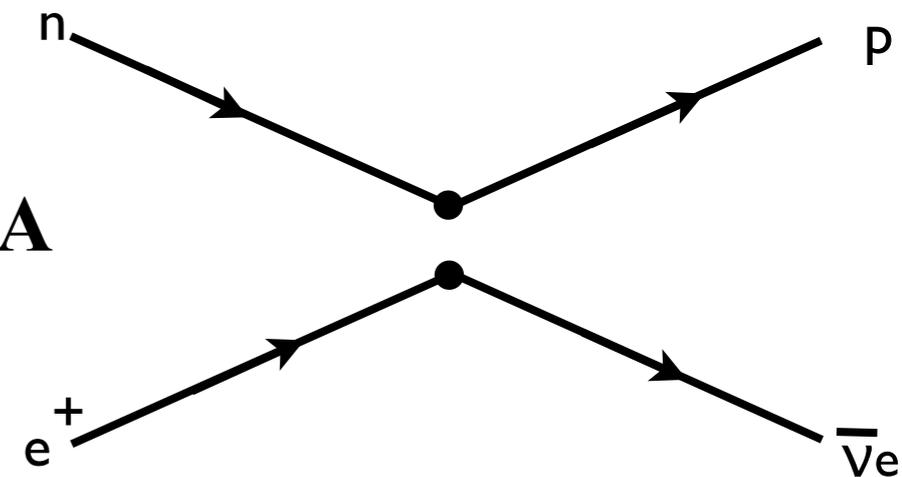
$$M_{weak-CC-Fermi} = G_F (\bar{u}_n\gamma^\mu u_p) (\bar{u}_\nu\gamma_\mu u_e)$$

G_F is weak coupling constant (Fermi constant)
 has dimensions GeV^{-2} (unlike charge, e)
 remains to be determined experimentally

V-A Form of Weak Current

$$M_{weak-CC-Fermi} = G_F (\bar{u}_n \gamma^\mu u_p) (\bar{u}_\nu \gamma_\mu u_e)$$

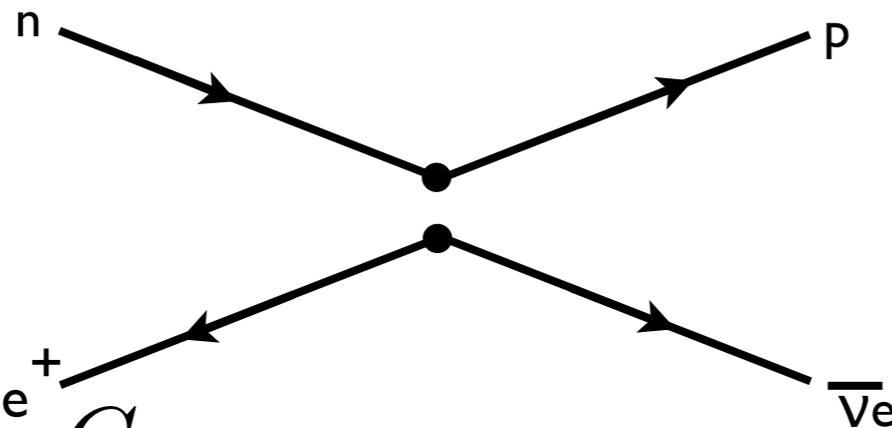
- Fermi's proposed amplitude explained properties of some features of β -decay, but not others!
- For next 25 years, a suite of β -decay experiments were performed to unravel true form of the weak interaction
- Discovery of Parity violation in 1956 !
- Change in Fermi's proposal: $\gamma^\mu \rightarrow \gamma^\mu(1-\gamma^5) \rightarrow \mathbf{V - A}$
 - γ^μ is vector \rightarrow inverts under Parity op.
 - γ^5 is pseudoscalar \rightarrow inverts under Parity op.
 - $\gamma^\mu \gamma^5$ is axial vector \rightarrow does not invert under Parity op.
- Mixture of γ^μ and $\gamma^\mu \gamma^5$ terms violates Parity in weak interactions !



V-A Form of Weak Current

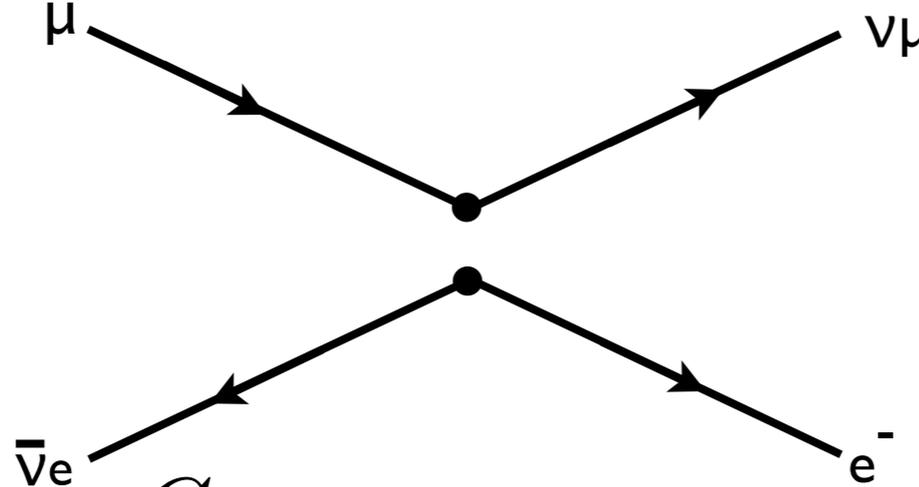
- Parity is not conserved in weak interactions :
 - Lee & Yang, Phys. Rev. 104, 254-258 (1956)
 - Explains $K \rightarrow 2\pi$ and 3π ; final states have opposite parities !
- Experimental verification : β -transitions of polarized Cobalt nuclei

β -decay



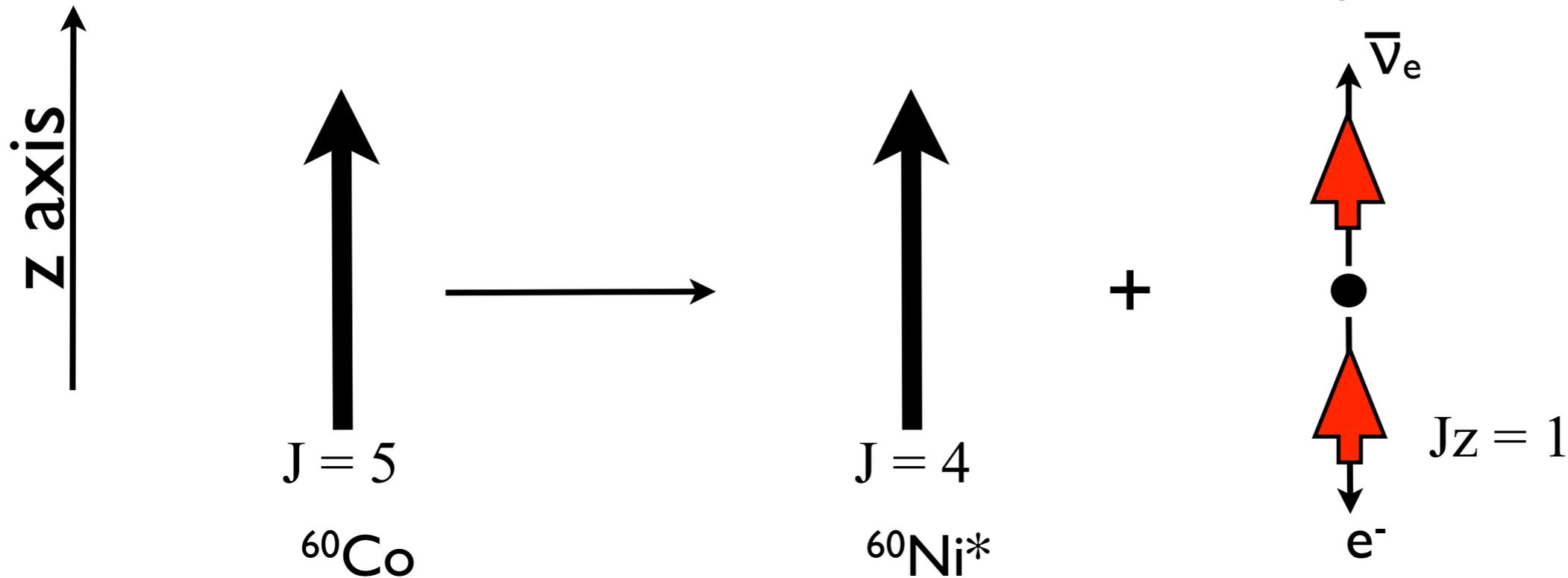
$$M (n \rightarrow p e^- \bar{\nu}_e) = \frac{G_F}{\sqrt{2}} (\bar{u}_n \gamma^\mu (1 - \gamma^5) u_p) (\bar{u}_{\nu_e} \gamma_\mu (1 - \gamma^5) u_e)$$

μ -decay



$$M (\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu) = \frac{G_F}{\sqrt{2}} (\bar{u}_{\nu_\mu} \gamma^\sigma (1 - \gamma^5) u_\mu) (\bar{u}_e \gamma_\sigma (1 - \gamma^5) u_{\nu_e})$$

Parity Violation Experiment with ^{60}Co



- Electron is emitted opposite in direction to spin of ^{60}Co !
- This asymmetry changed sign upon magnetic field reversal !
- Observed correlation explained by assuming RH(positive helicity) antineutrino and LH(negative helicity) electron !
- $(1-\gamma^5)$ automatically selects a LH neutrino or a RH antineutrino !

Parity Violation Experiment with ^{60}Co

- Weak interactions involve ONLY ν_L & anti- ν_R
- LH neutrinos and RH antineutrinos couple to charged leptons in weak int.
- Absence of “mirror image” states is a clear violation of Parity
- NO empirical evidence for anti- ν_L & ν_R
- Charge conjugation invariance is also violated (else $\nu_L \rightarrow$ anti- ν_L)
- Weak interaction is invariant under CP operation

$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) \neq \Gamma(\pi^+ \rightarrow \mu^+ \nu_R) \quad \dots \text{P violation}$$

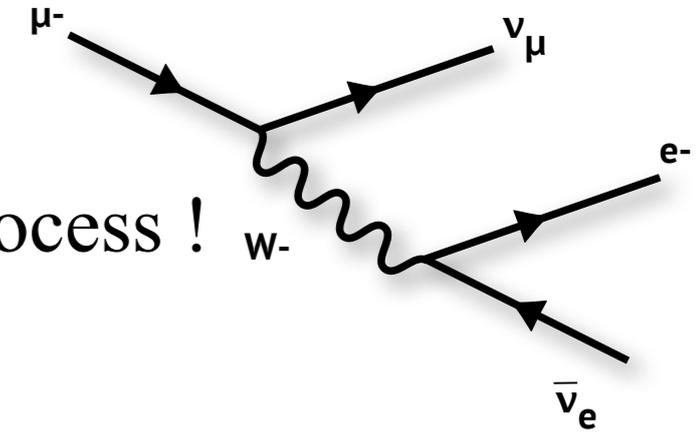
$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) \neq \Gamma(\pi^- \rightarrow \mu^- \bar{\nu}_L) \quad \dots \text{C violation}$$

$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) = \Gamma(\pi^- \rightarrow \mu^- \bar{\nu}_R) \quad \dots \text{CP invariance}$$

- Although future experiments will look for CP violation in neutrinos !

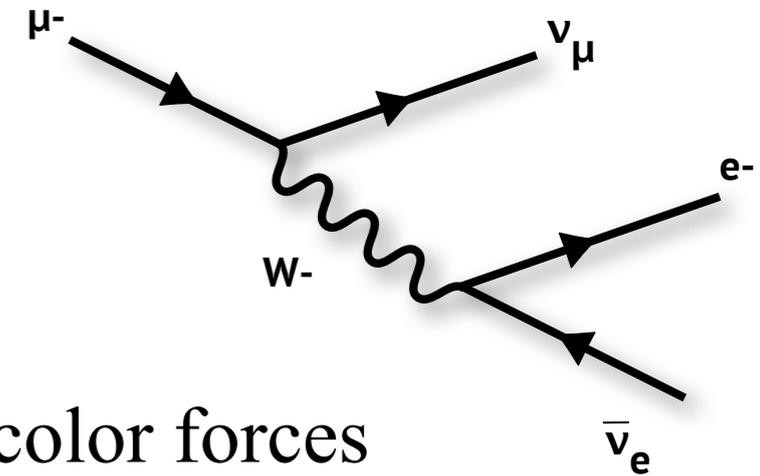
Interpretation of the Coupling Constant G_F

- Crucial check of the universality of the strength of G_F
- We do not want a new interaction for every weak process !
- In Fermi's model of EM and weak interactions:
 - Analogy: G_F essentially replaces e^2/q^2 (G_F dimensions GeV^{-2})
 - Weak interactions involve emission & absorption of vector bosons
 - Weak bosons Z, W^\pm



Act of “throwing” or “catching” the boson also transforms the particles !

Interpretation of the Coupling Constant G_F



- W^\pm are analogues of γ for EM forces and gluons for color forces

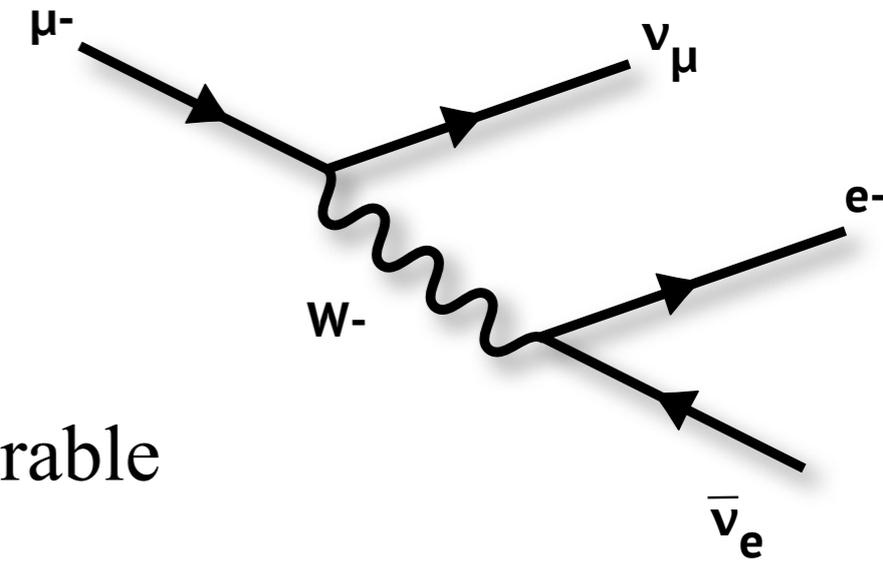
$$M_{\text{MuonDecay}} = \left(\frac{g}{\sqrt{2}} \bar{u}_{\nu_\mu} \gamma^\sigma \frac{1}{2} (1 - \gamma^5) u_\mu \right) \frac{1}{M_W^2 - q^2} \left(\frac{g}{\sqrt{2}} \bar{u}_e \gamma_\sigma \frac{1}{2} (1 - \gamma^5) u_{\nu_e} \right)$$

- $g/\sqrt{2} \rightarrow$ dimensionless weak coupling; $q \rightarrow$ momentum of W boson
- $M_W \sim 80 \text{ GeV}$ (else it would be directly produced in weak decays!)
- In β -decay & μ -decay: $q^2 \ll M_W^2$

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2}$$

- Weak interactions are “weak” because M_W^2 is large (not because $g \ll e$) !

Universality of G_F

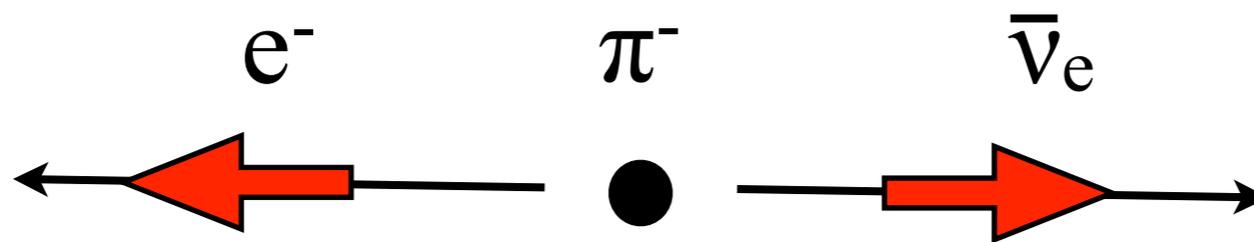


- If $g \approx e$: weak & EM interactions will be of comparable strength at energies $\geq O(M_W)$
- Unification of weak and EM interactions \rightarrow electroweak
- Observed rates of β and μ decays can be used to estimate G_F
 - From nuclear β -decays: $G_F = 1.136 \times 10^{-5} \text{ GeV}^{-2}$
 - From muon decays: $G_F = 1.166 \times 10^{-5} \text{ GeV}^{-2}$
- Supports assertion of the universality of G_F !
 - Nuclear β -decay and muon decay have the same physical origin !
 - Small difference is due to quark-mixing ($\cos\theta_c$)

Pion Decay

$$\frac{\Gamma(\pi^- \rightarrow e^- \bar{\nu}_e)}{\Gamma(\pi^- \rightarrow \mu^- \bar{\nu}_\mu)} = 1.2 * 10^{-4}$$

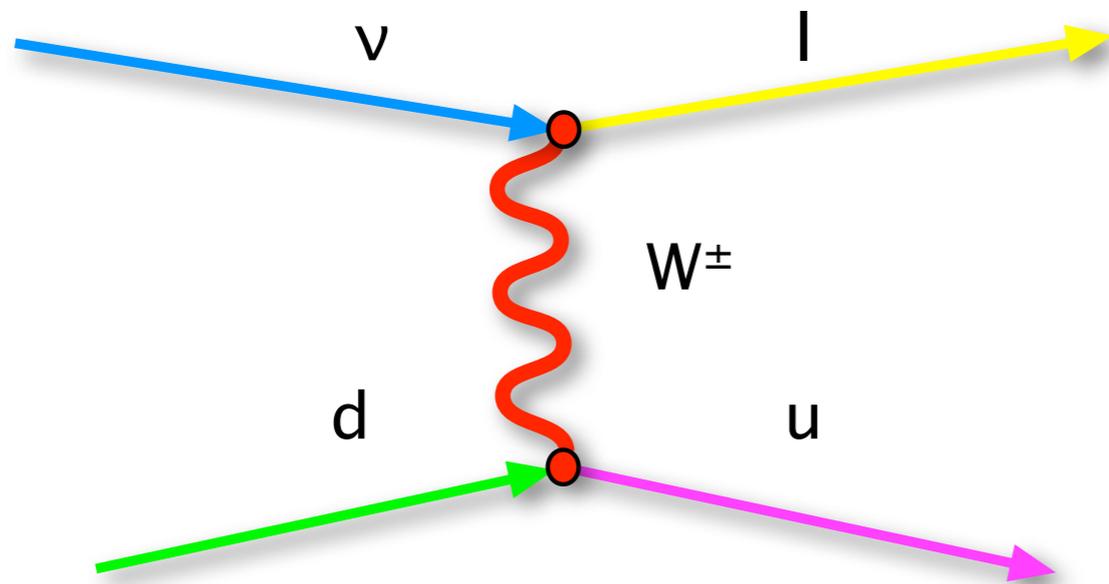
- π^- prefers to decay into a muon (similar mass) rather than electron (much lighter) ! Why ?



- Conservation of angular momentum must have $J=0$ for outgoing lepton pair
- Forces μ^- (e^-) to have a positive helicity - “wrong” helicity state for μ^- (e^-) !
- As $m_e \rightarrow 0$, weak current only couples negative helicity e^- , hence positive helicity coupling is suppressed !
- “Wrong” helicity state is much more likely to happen for μ^- than e^-
- Is a direct consequence of $(1-\gamma^5)$ structure of weak current!

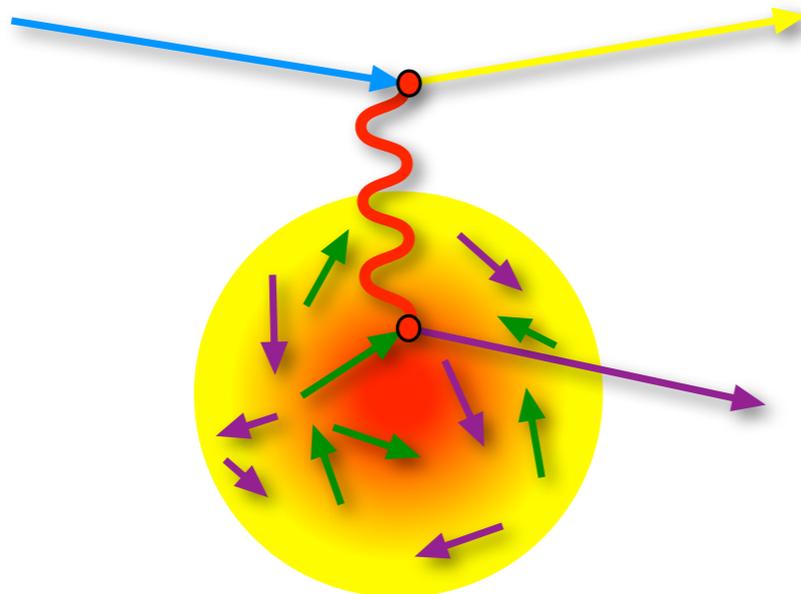
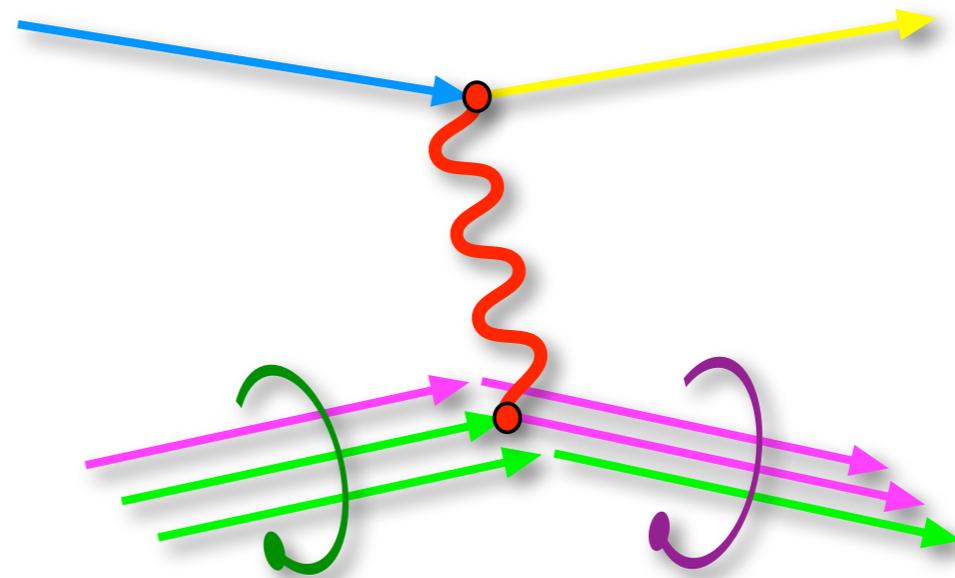
A Recap of Discussions so far

- Neutrinos interact via weak interactions only !
- All hadrons and leptons experience weak interaction
 - But they're often hidden by the strong and EM interactions
- Form of weak current first derived by Fermi (point interaction)
- Discovery of Parity violation in 1956 !
- Change in Fermi's proposal: $\gamma^\mu \rightarrow \gamma^\mu(1-\gamma^5) \rightarrow \mathbf{V} - \mathbf{A}$
- Mixture of γ^μ and $\gamma^\mu \gamma^5$ terms violates Parity in weak interactions !
- Parity violation experimentally confirmed by Madam Wu.
- Weak interactions involve ONLY ν_L & anti- ν_R
- Weak interactions are CP invariant until you start looking for CP violation
- Fermi's constant G_F is universal, M_W important contributor
- Pion decays to muon preferentially - positive helicity is suppressed more for electron than muon



Neutrino-lepton and neutrino quark scattering are tractable. Simpler topologies dealing with fundamental particles.

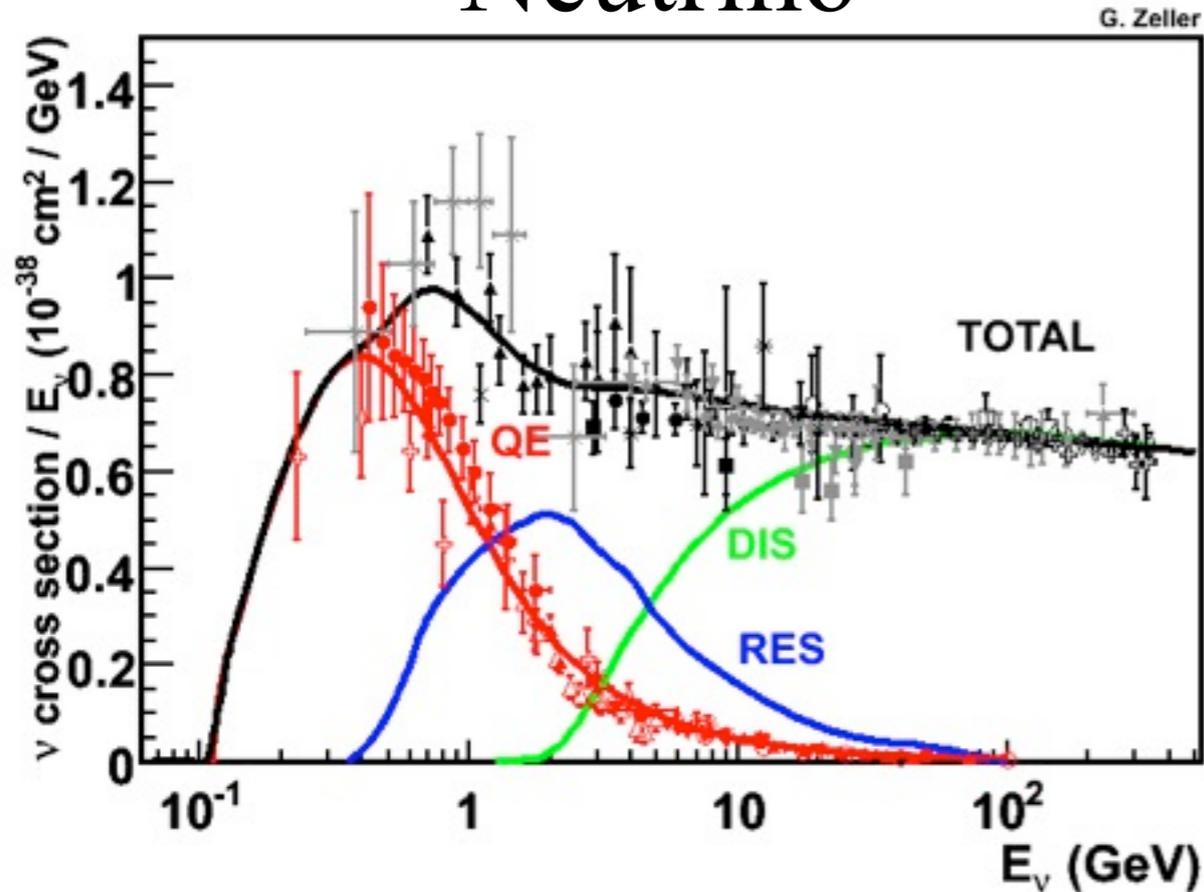
Neutrino-nucleon starts getting complex ! Nuclear medium poses challenges. Parametrization with help of form factors part of recipe.



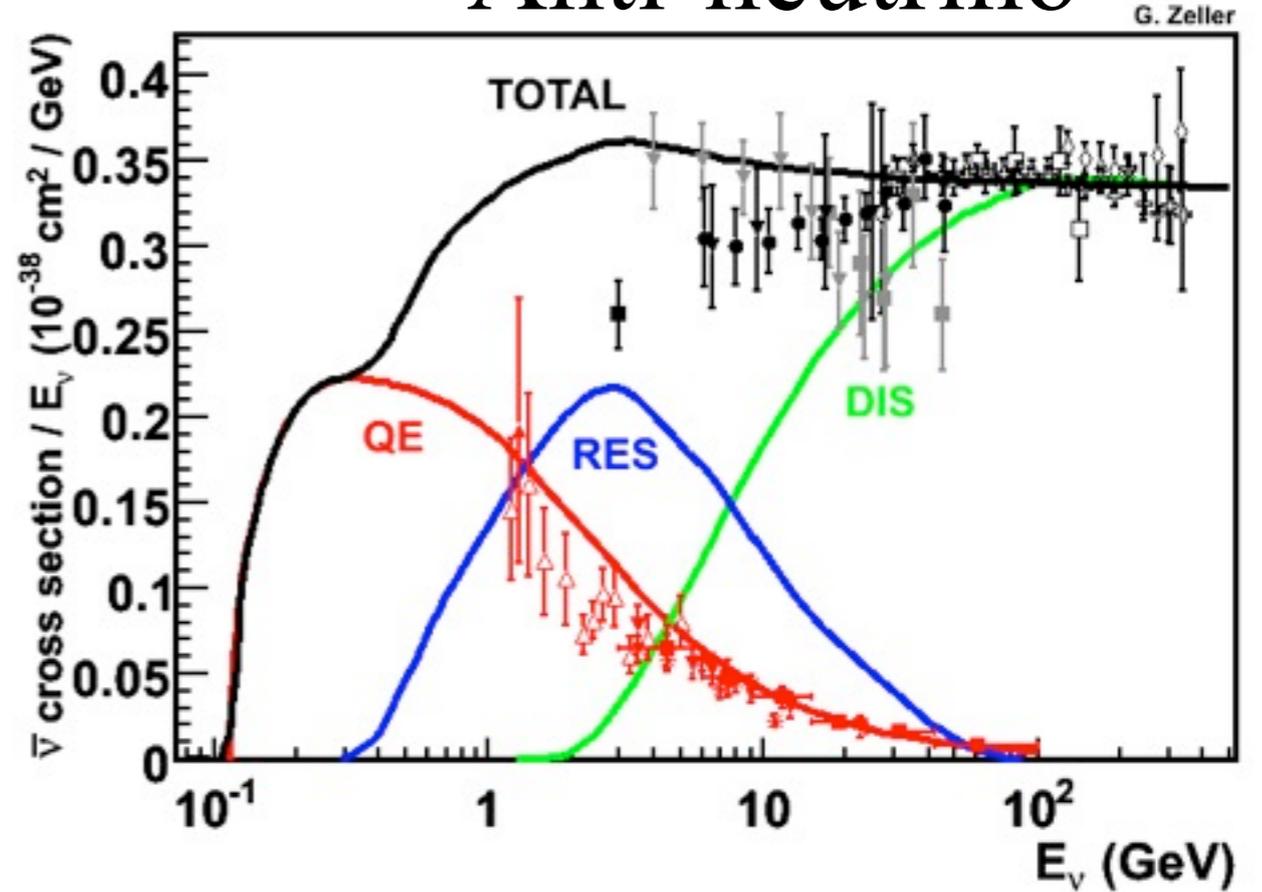
Neutrino-nucleus becomes very complex ! But this is where we want σ

Neutrino cross-sections

Neutrino



Anti-neutrino

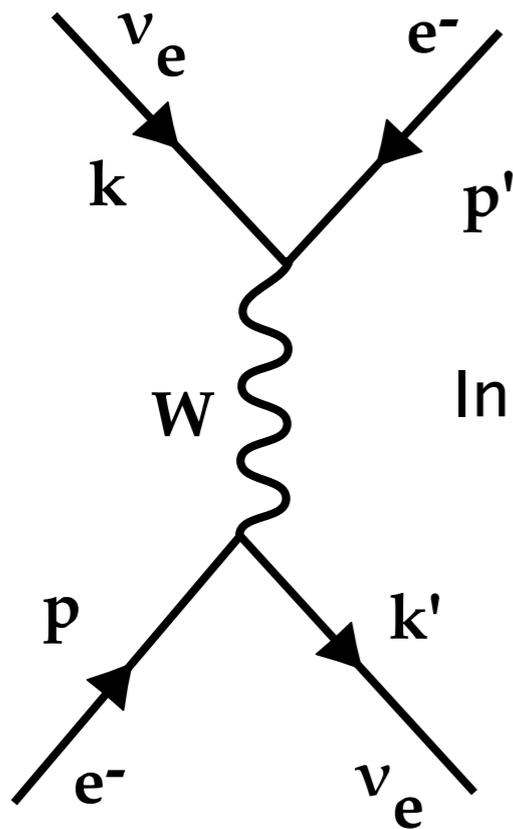


The most important distinctions are with respect to final state multiplicity, pion production and kinematics (Q^2 , W , etc.)

J.A. Formaggio and G.P. Zeller, "From eV to EeV: Neutrino Cross Sections Across Energy Scales", to be published in Rev. Mod. Phys. 2012

Charged Current Neutrino-Electron Scattering

Neutrino-Electron Scattering



$$\mathcal{M} = \frac{G_F}{2} (\bar{u}(k') \gamma^\mu (1 - \gamma^5) u(p)) (\bar{u}(p') \gamma^\mu (1 - \gamma^5) u(k))$$

In relativistic limit: $m_e = 0$ & $s = (k + p)^2 = 2k \cdot p = 2k' \cdot p'$

$$\frac{1}{2} \sum_{spins} |\mathcal{M}|^2 = 64G_F^2 (k \cdot p) (k' \cdot p')$$

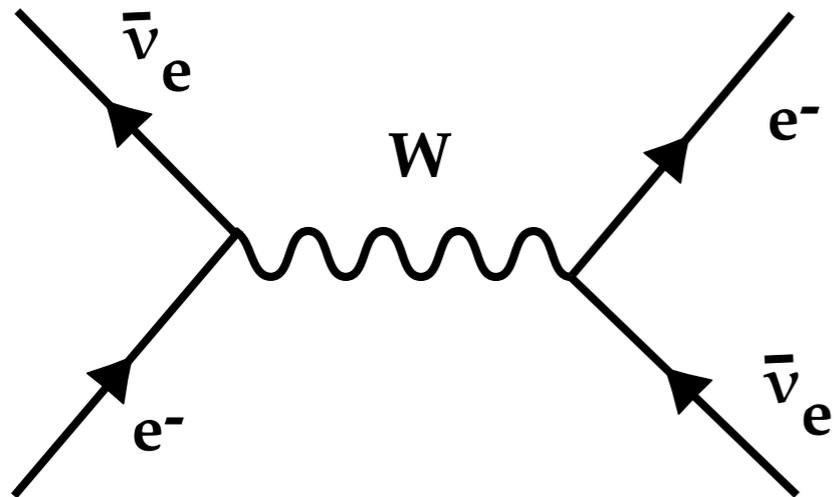
$$= 16G_F^2 s^2$$

Skip a lot of steps! See: Halzen & Martin Quarks & Leptons or Griffiths Intro. to Elementary Particles.

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s} \overline{|\mathcal{M}|^2} = \frac{G_F^2 s}{4\pi^2} \implies \sigma = \frac{G_F^2 s}{\pi}$$

Antineutrino- Electron Scattering

By crossing the neutrinos of previous diagram, we have the result, replacing s with t :



$$\begin{aligned}\frac{1}{2} \sum_{spins} |\mathcal{M}|^2 &= 16G_F^2 t^2 \\ &= 4G_F^2 s^2 (1 - \cos \theta)^2\end{aligned}$$

θ is the opening angle between incoming $\bar{\nu}_e$ and outgoing e^-

Integrating over angles, we have:

$$\frac{d\sigma}{d\Omega} = \frac{G_F^2 s}{16\pi^2} (1 - \cos \theta)^2 \implies \sigma = \frac{G_F^2 s}{3\pi}$$

Why the factor of 3 ?

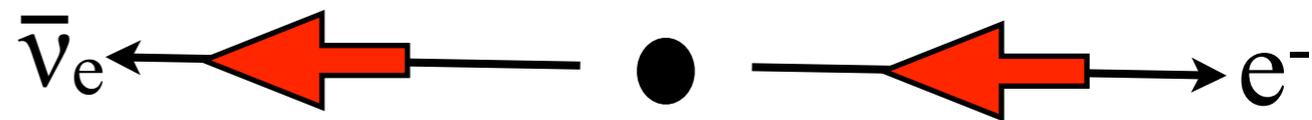
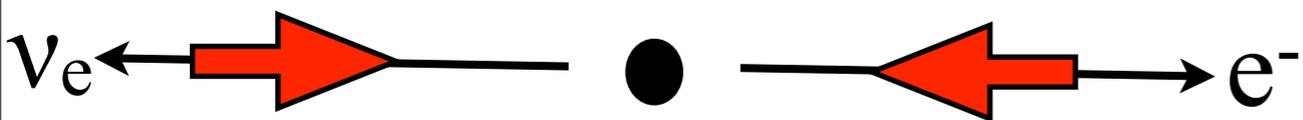
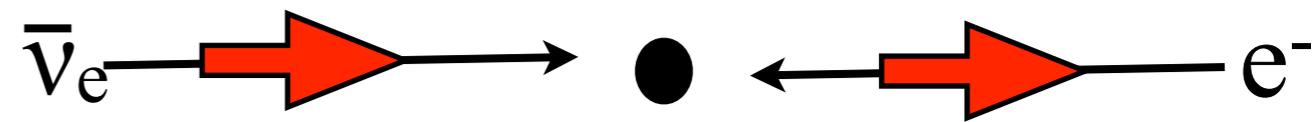
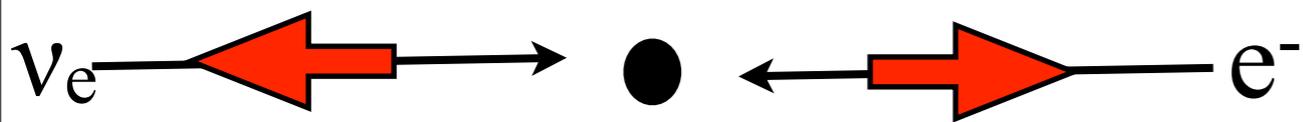
$$\sigma(\bar{\nu}_e e^-) = \frac{1}{3} \sigma(\nu_e e^-)$$

$$\frac{d\sigma}{d\Omega}(\nu_e e^-) = \frac{G_F^2 s}{4\pi^2}$$

does not vanish !

$$\frac{d\sigma}{d\Omega}(\bar{\nu}_e e^-) = \frac{G_F^2 s}{16\pi^2} (1 - \cos\theta)^2$$

vanishes for $\cos\theta = 1$!



$(J_z)_i = (J_z)_f = 0$
Allowed

$(J_z)_i = +1; (J_z)_f = -1$
Forbidden

- Backward anti- ν_e scattering is forbidden !
- Scattering proceeds entirely in $J=1$ state, net helicity +1

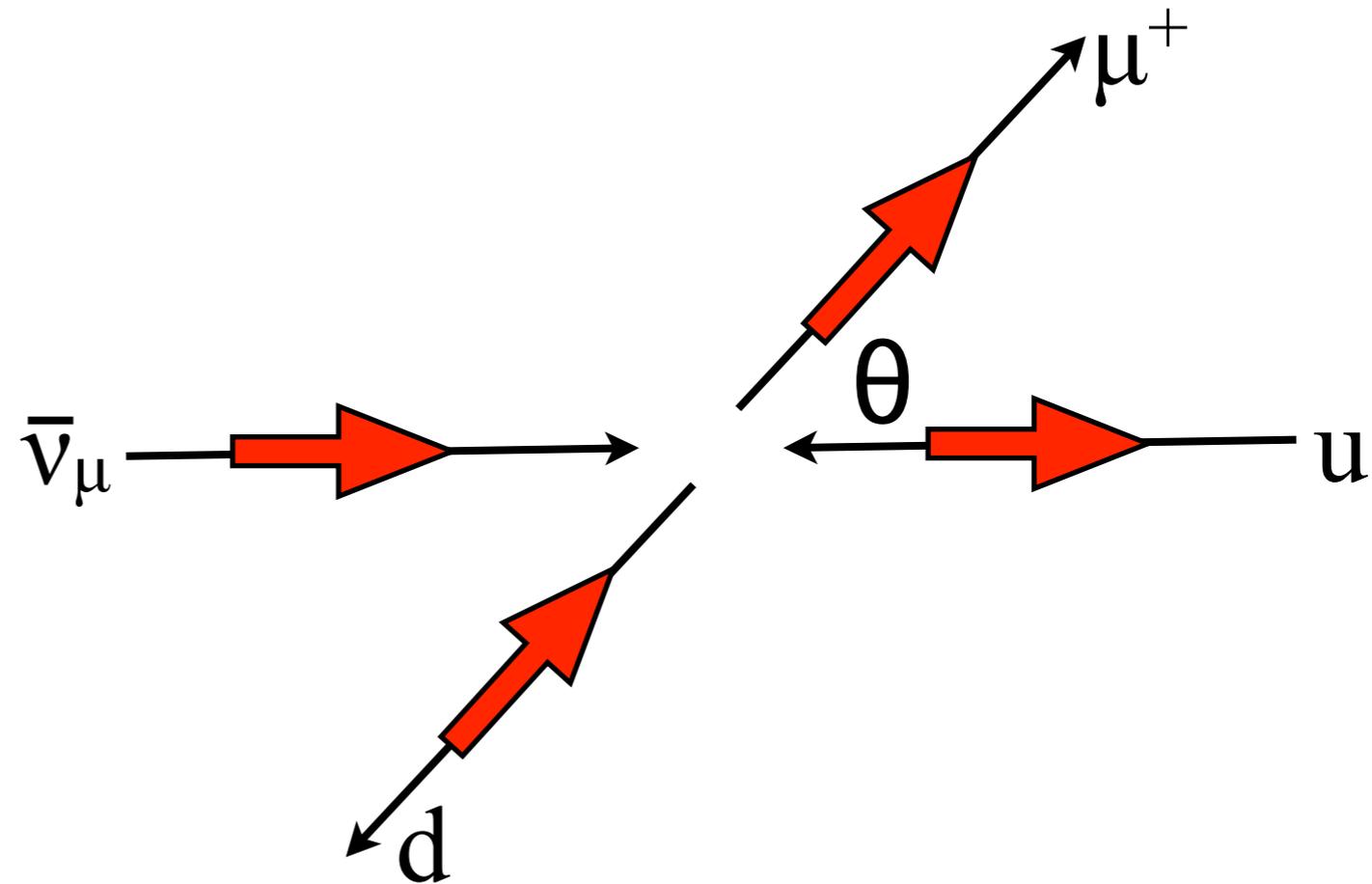
Charged Current Neutrino-Quark Scattering

Neutrino Quark Scattering

$$\frac{d\sigma}{d\Omega} (\nu_{\mu} d \rightarrow \mu^{-} u) = \frac{G_F^2 s}{4\pi^2}$$

$$\frac{d\sigma}{d\Omega} (\bar{\nu}_{\mu} u \rightarrow \mu^{+} d) = \frac{G_F^2 s}{16\pi^2} (1 + \cos\theta)^2$$

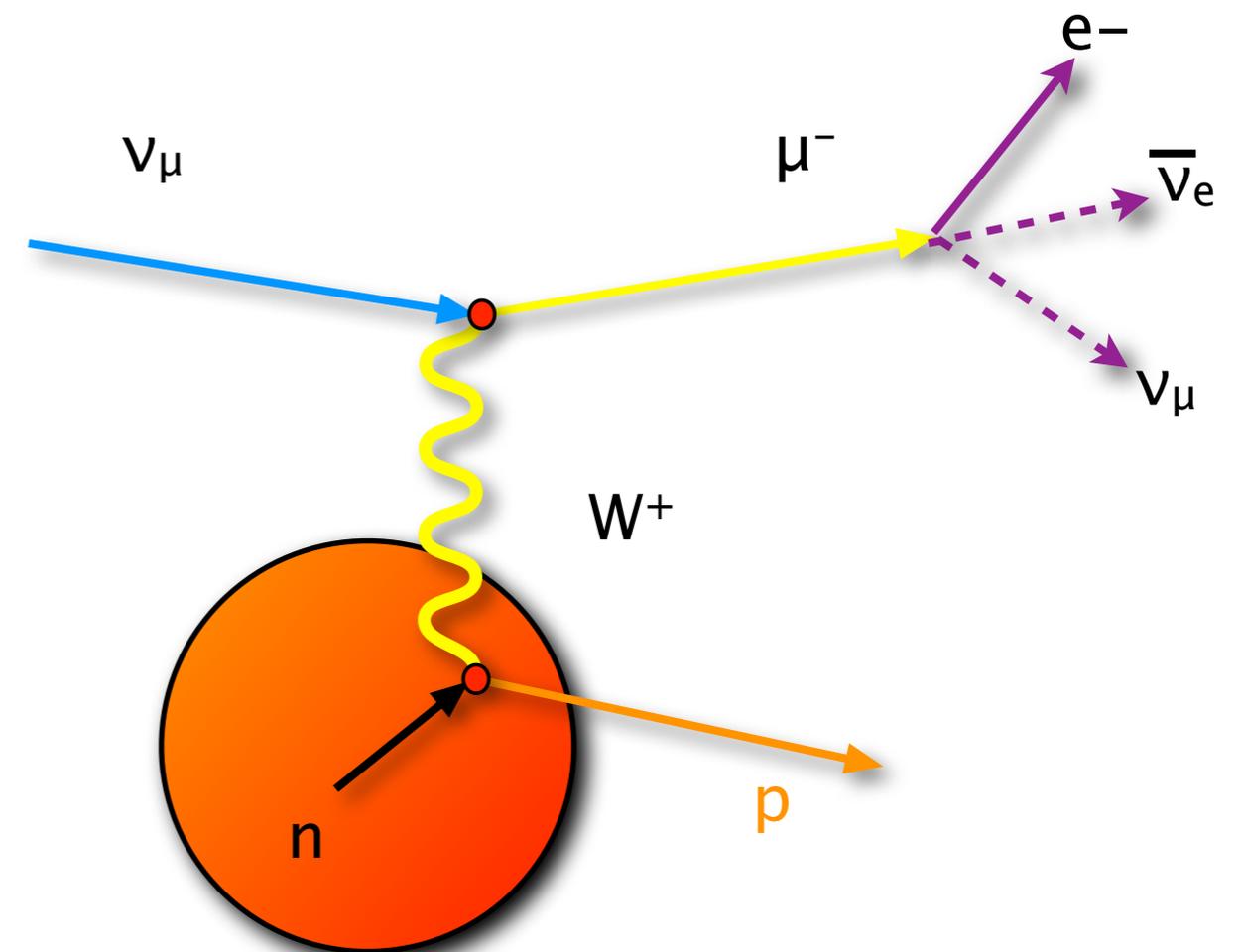
- Backward scattering ($\theta=\pi$) is forbidden by helicity considerations !
- These constituent x-secs are embedded in νN inclusive cross-sections for comparing with exptl. results (e.g. DIS)



Neutrino Quasi-Elastic Scattering

Why is $\nu(\bar{\nu})$ -QE scattering important ?

- Flagship signal channel in current and future generation neutrino oscillation experiments
- For ν_e appearance we need a simple final state
- Interaction with a free nucleon is tractable (compared to DIS)
 - Actually not that simple when compare results with predictions
 - Nuclear effects and form factors make it challenging
- Improve phenomenological models & dictionaries of events

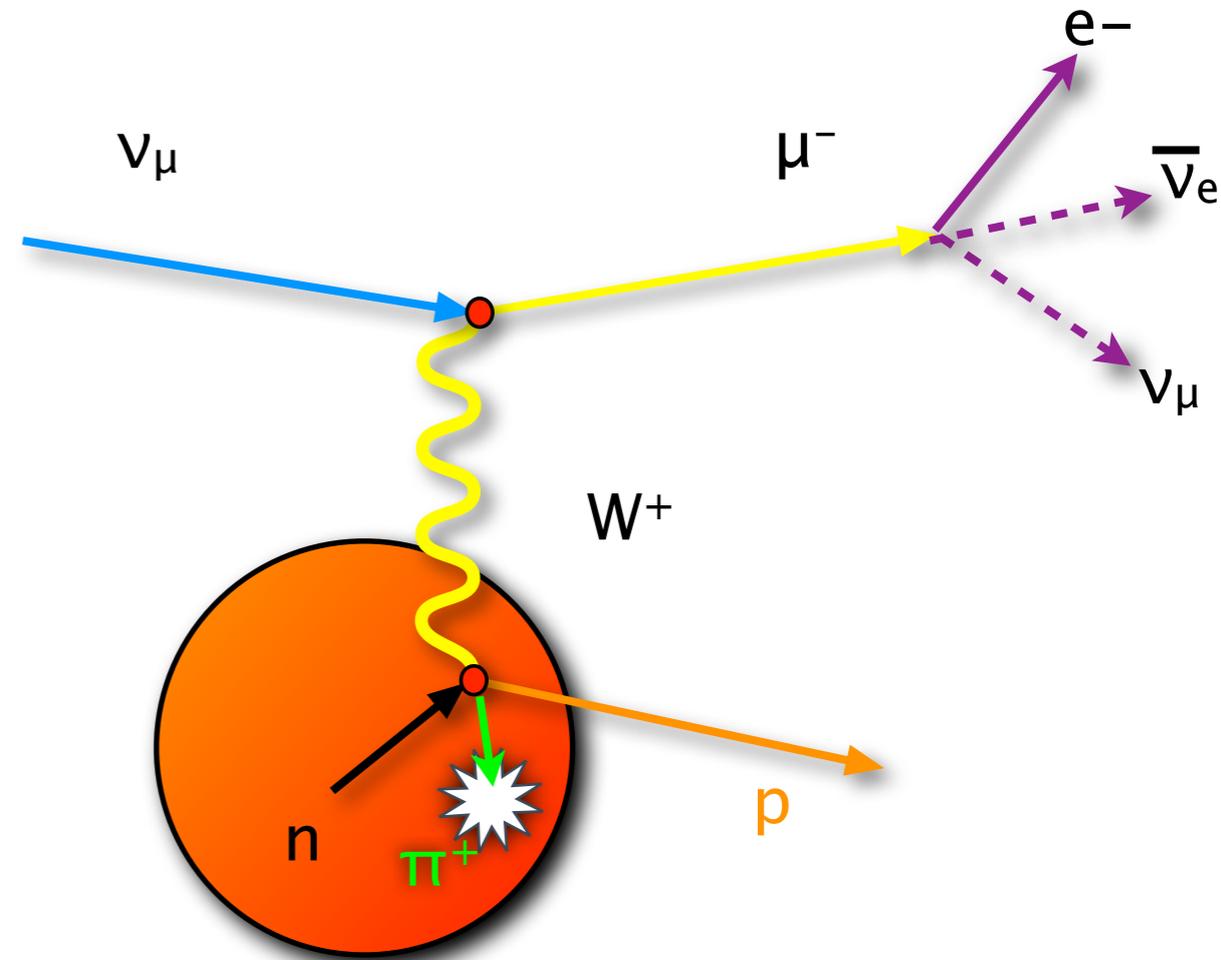


$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$

Characteristics of QE Scattering

- Neutrino energy and flavor inferred from just the lepton kinematics !
- Muon decay (Michel) electron helps with particle ID in some detectors
- Main background is $CC1\pi^+$ (e.g. resonance) where pion is undetected
- Backgrounds create a bias in parameter estimation for oscillation experiments. They depend on a good understanding of E_ν !



W^\pm

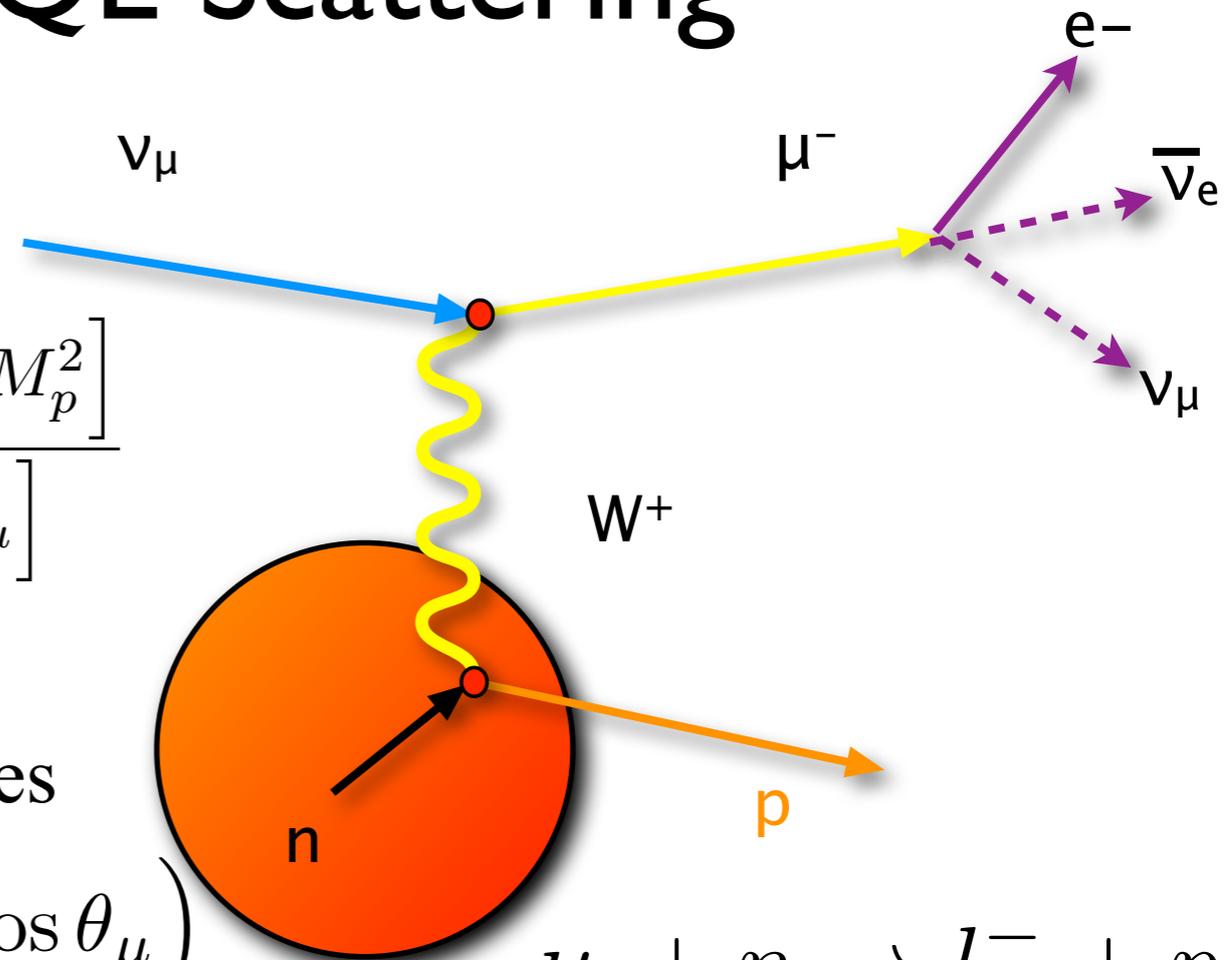
Characteristics of QE Scattering

Neutrino energy from Muon variables

$$E_{\nu}^{QE} = \frac{2(M_n - E_B) E_{\mu} - \left[(M_n - E_B)^2 + m_{\mu}^2 - M_p^2 \right]}{2 \left[(M_n - E_B) - E_{\mu} + \sqrt{E_{\mu}^2 - m_{\mu}^2} \cos \theta_{\mu} \right]}$$

Four Momentum Transfer from Muon variables

$$Q_{QE}^2 = -m_{\mu}^2 + 2E_{\nu}^{QE} \left(E_{\mu} - \sqrt{E_{\mu}^2 - m_{\mu}^2} \cos \theta_{\mu} \right)$$



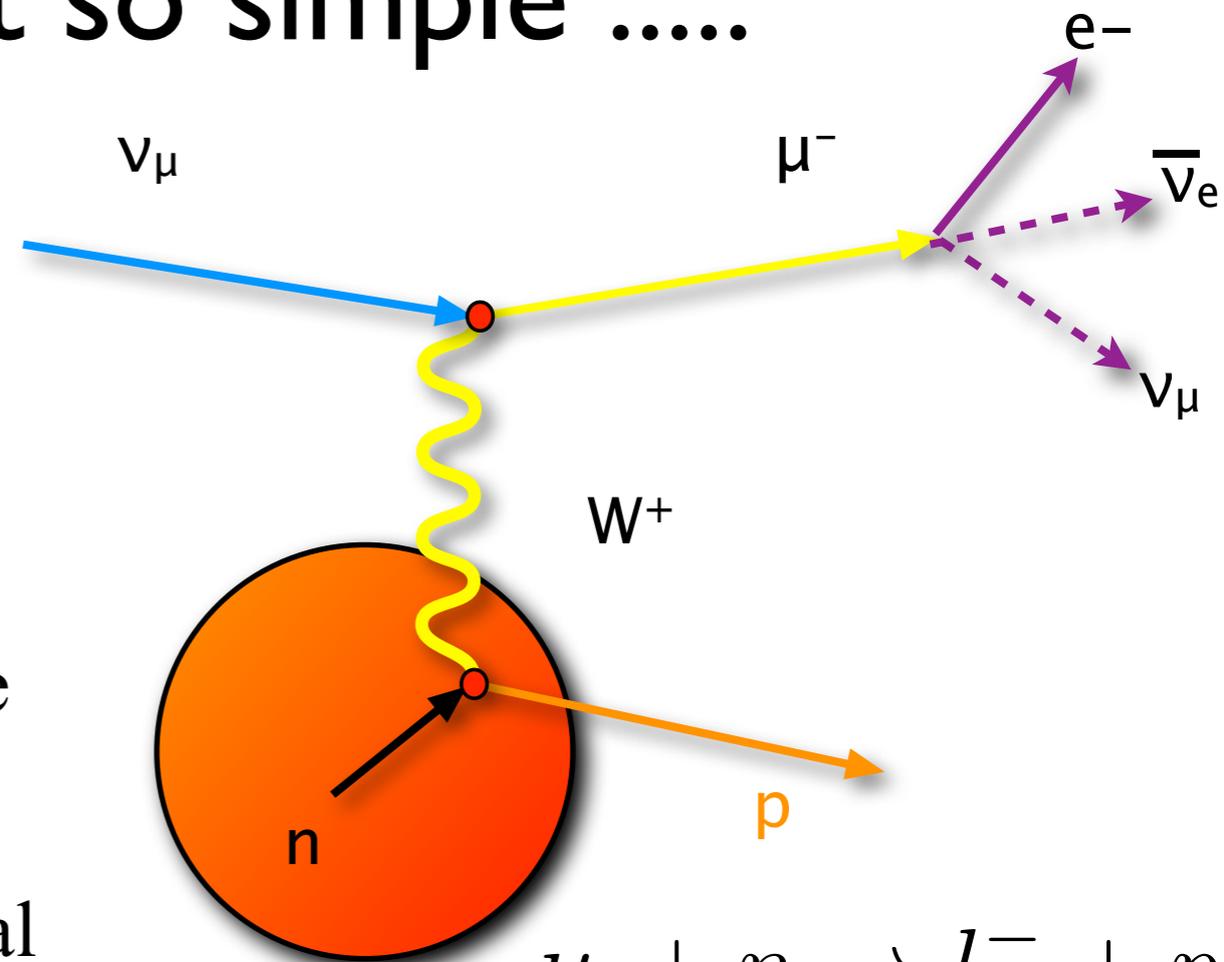
$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$

$E_{\mu} = T_{\mu} + m_{\mu}$	Muon Energy
M_n, M_p, m_{μ}	Neutron, Proton, Muon Mass
E_B	Binding Energy (~ 30 MeV)
θ_{μ}	Muon Angle w.r.t. Neutrino Direction

QE Scattering - not so simple

- Formalism works for free nucleons
- Nuclear medium makes it complex
- What structure does the neutrino resolve in the nucleus ?
- What would be a consistent experimental definition ?
- Different for nucleon & nucleus ?
- We also assume that nucleons are at rest
- Not true ! Moreover nucleons are off-shell & transition matrix elements are not known !

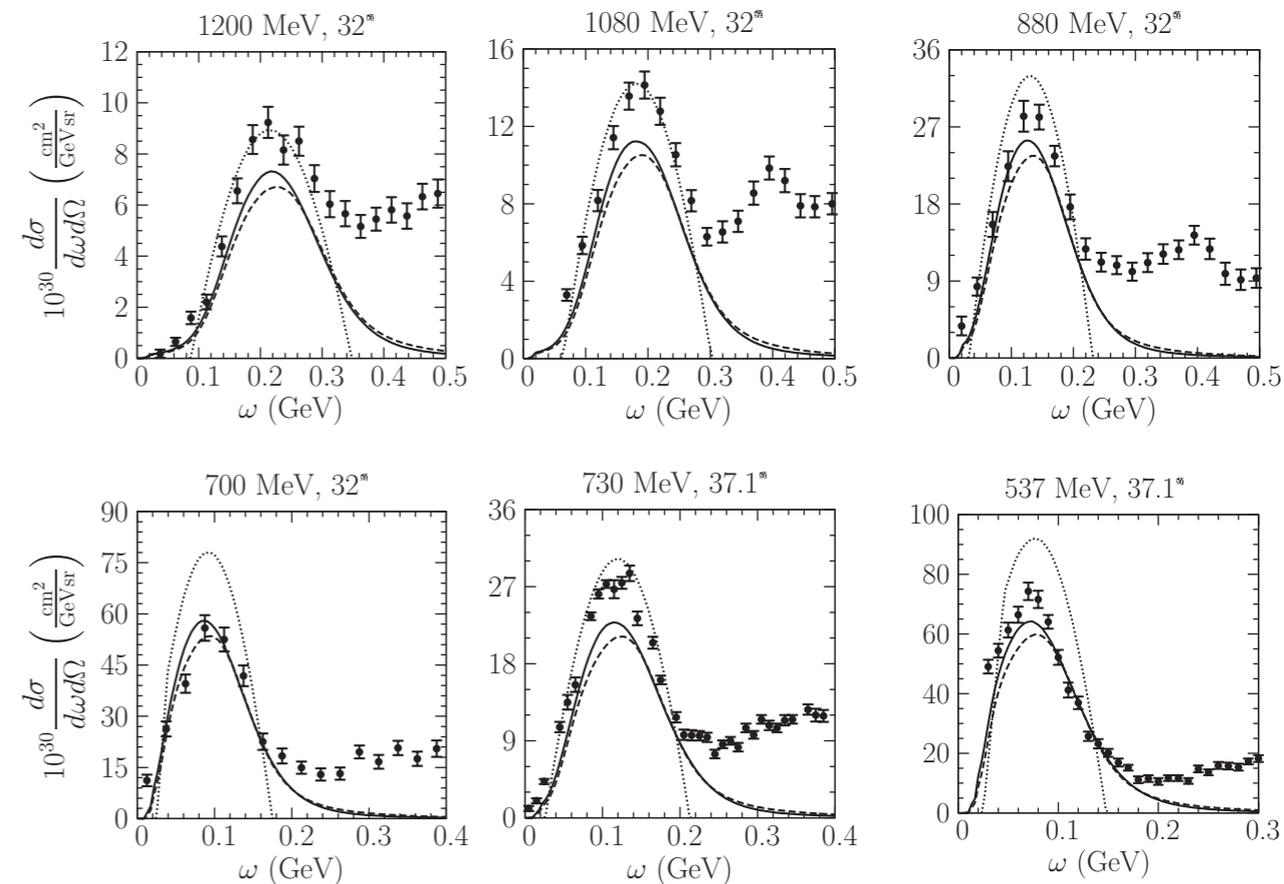
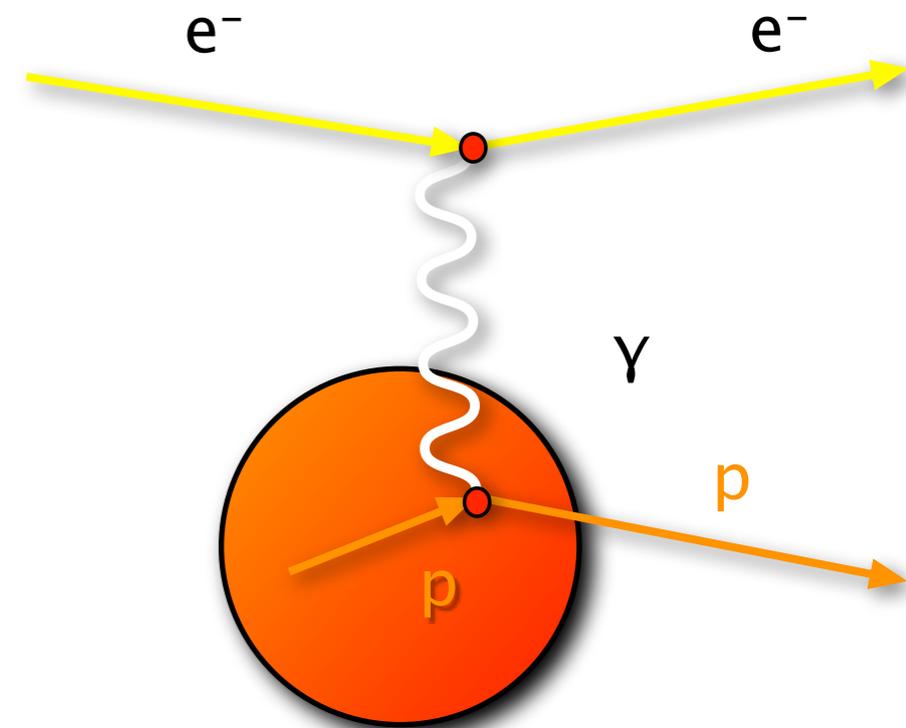


$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$

QE Scattering in electrons

- We know incoming and outgoing electron energies - great advantage !
- Very clear signature in electron scattering.
- Energy transfer is very sharply peaked as a function of angle and electron energy, with broadening due to initial state momentum.



Ankowski et al, Phys. Rev. C 77, 044311 (2008)

QE Scattering - Llewellyn Smith formalism

ν Cross Section:
$$\frac{d\sigma}{dQ^2} = \frac{M^2 G_F^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[A(Q^2) \pm B(Q^2) \frac{s-u}{M^2} + C(Q^2) \frac{(s-u)^2}{M^4} \right]$$

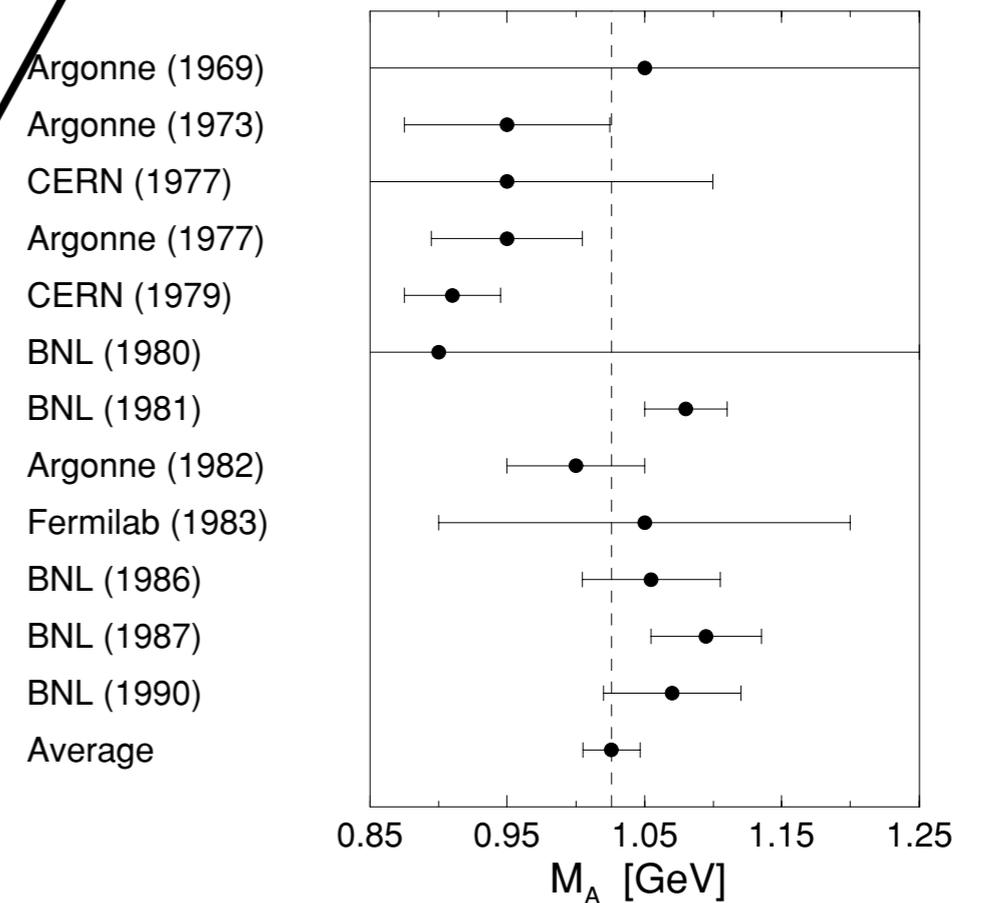
- Early formalism by Llewellyn Smith
- Vector and Axial-Vector components
- Vector piece can be lifted from well-studied electron scattering data.
- Neutrino experiments determine the Axial piece !
- Q^2 is the four-momentum transfer
- s and u are Mandelstam variables
- Lepton vertex is known. Nucleon structure is parameterized with 2 vector (F_1, F_2) and 1 axial-vector (F_A) form factors

C. H. Llewellyn Smith, Phys. Rep. C3 261 (1972).

Llewellyn Smith & CCQE Cross Sections

- Standard Application:
 - **Assume** a Fermi Gas Model with parameters from electron scattering (or a favorite nuclear model).
 - Typically (FGM) **assume** the Impulse Approximation.
 - Vector form factors from electron scattering.
 - **Assume** dipole form for Axial-vector form factor. **Everything now follows from M_A .** Measure the x-section, get M_A .
 - $F_A(0)$ is measured in beta-decay.
- Early measurements of F_A involved low statistics on light targets (deuterium) at high energy.

$$F_A(Q^2) = \frac{-g_A}{(1 + Q^2/M_A^2)^2}$$



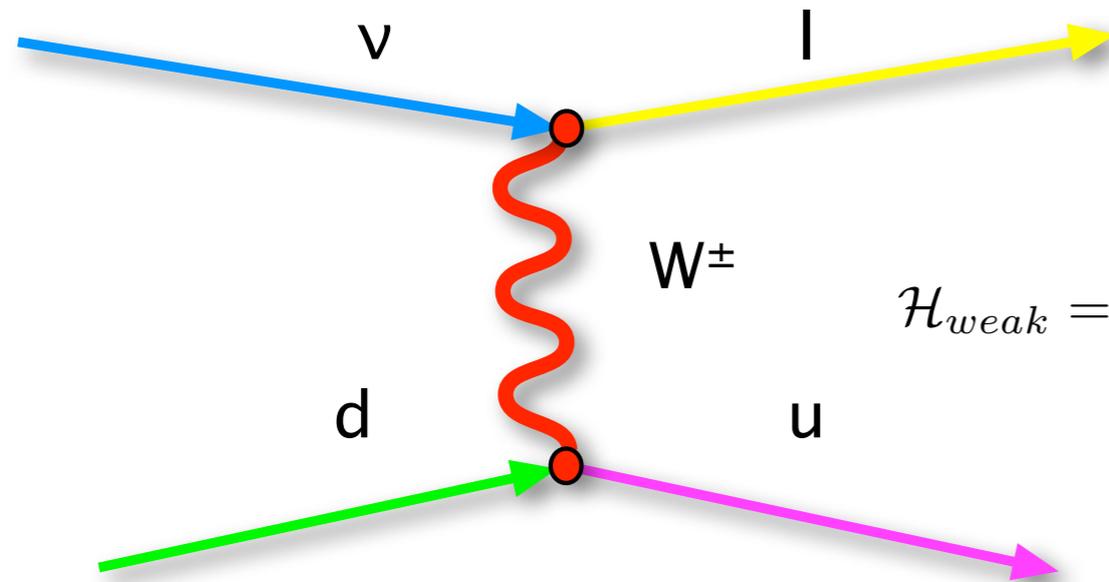
Bernard et al 2002 J. Phys. G: Nucl. Part. Phys. 28 R1

Relativistic Fermi Gas: Smith, Moniz, NPB 43, 605 (1972)

Llewellyn Smith, C.H., 1972, Phys. Rep. C3, 261.

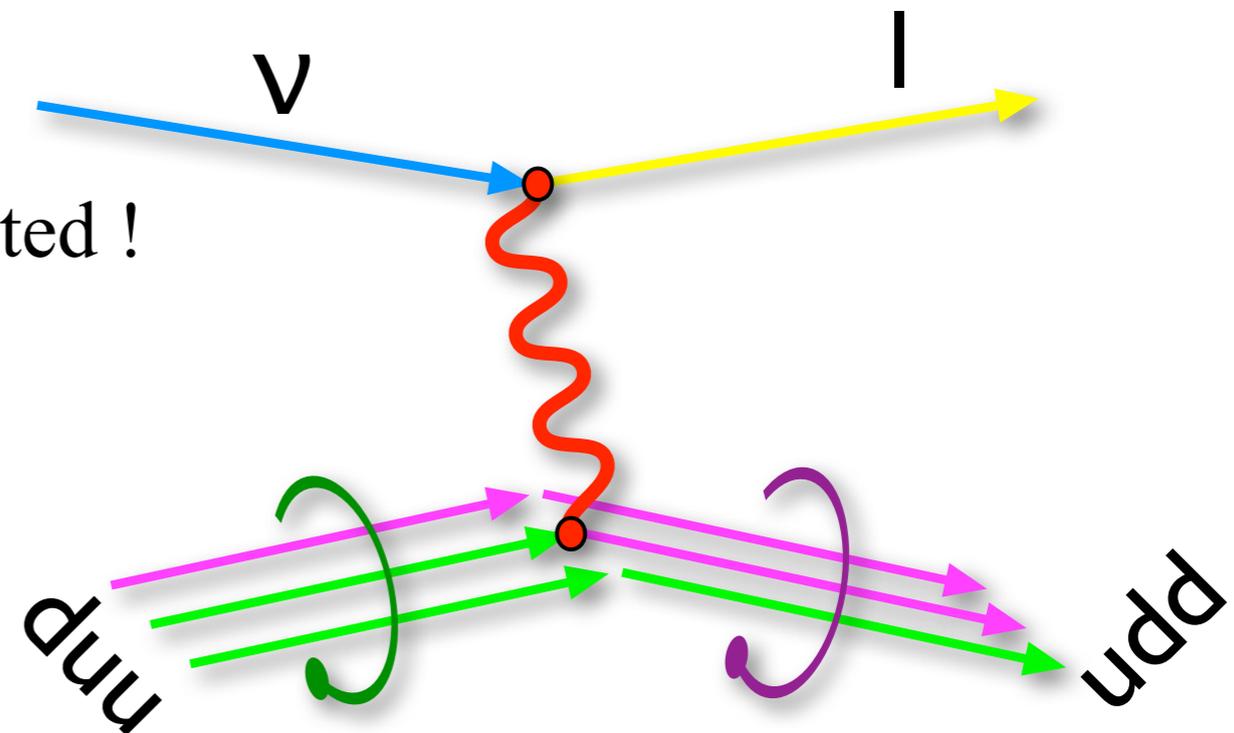
Axial Form Factor & M_A

“Intuition” for the axial form factor & M_A



We know how to handle scattering for Dirac particles:

$$\mathcal{H}_{weak} = \frac{4 G_F}{\sqrt{2}} \left[\bar{l}/\bar{\nu} \gamma_\mu \frac{1 - \gamma_5}{2} \nu \right] \left[\bar{f}' \gamma_\mu \left(g_L \frac{1 - \gamma_5}{2} + g_R \frac{1 + \gamma_5}{2} \right) f \right] + h.c.$$



In real protons things get more complicated !

Form Factor : Fourier Transform of the Charge Distribution

$$\rho(r) = \rho_0 e^{-mr}$$

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Fourier Transform of the Charge
Distribution

$$\rho(r) = \rho_0 e^{-mr}$$

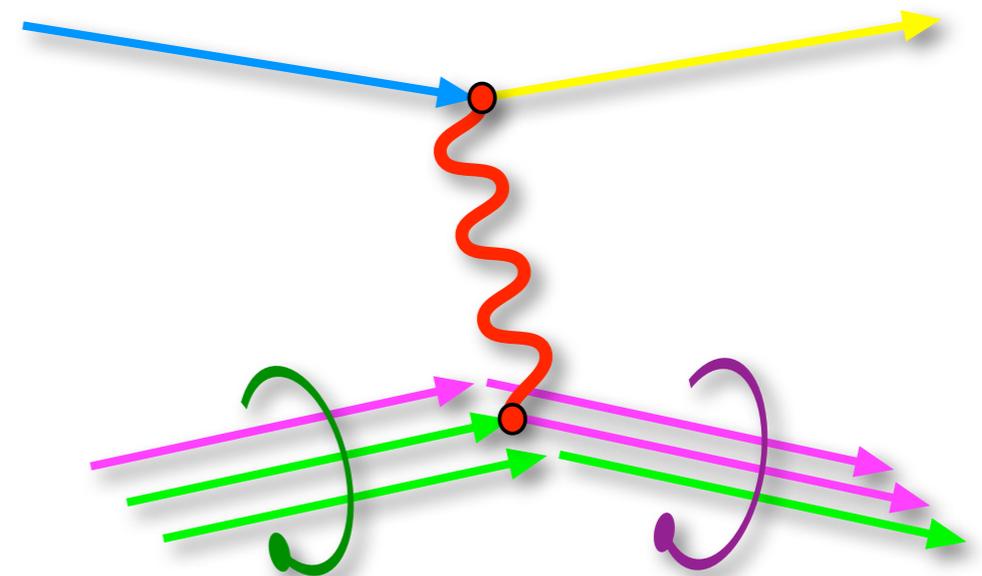
m is a constant

$$\begin{aligned} F(|q|^2) &= N \int e^{-mr} e^{i\vec{q} \cdot \vec{x}} d^3x \\ &= 2\pi N \int r^2 e^{-mr} e^{i|q|r \cos \theta} dr d(\cos \theta) \\ &= \frac{2\pi N}{i|q|} \int_0^\infty r \left[e^{-(m-i|q|)r} - e^{-(m+i|q|)r} \right] dr \\ &= \frac{8\pi N}{m^3 \left(1 + \frac{|q|^2}{m^2} \right)^2} \end{aligned}$$

Normalization:

$$N \int e^{-mr} d^3x = 1 \Rightarrow N = m^3 / 8\pi$$

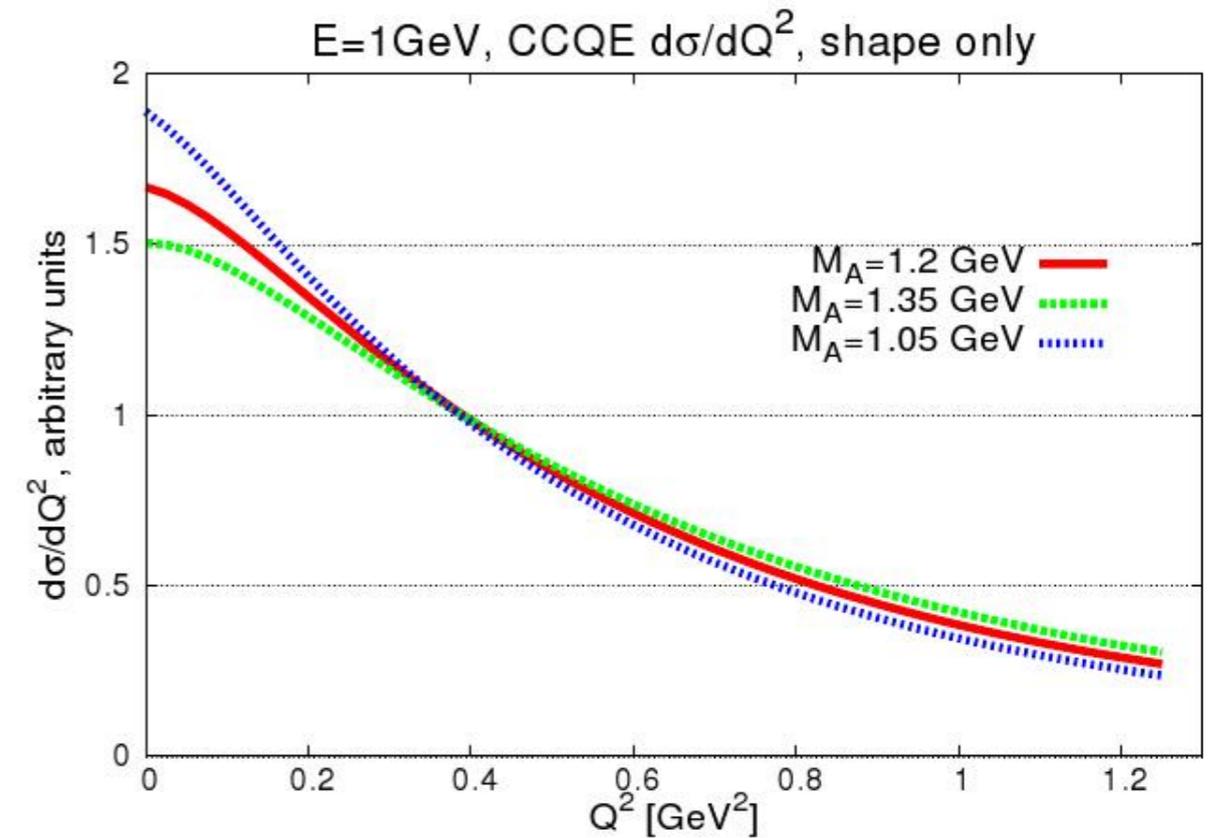
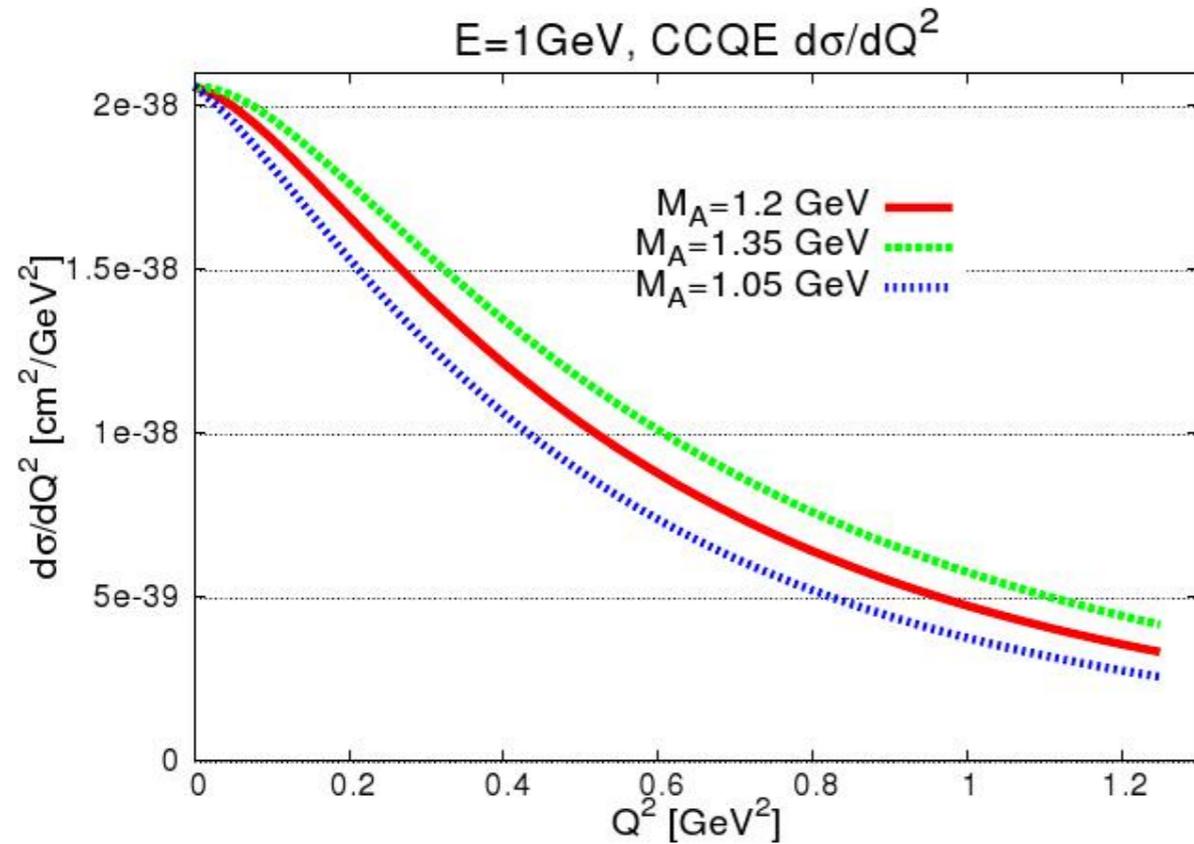
$$\Rightarrow F(q^2) = \frac{1}{\left(1 - \frac{q^2}{m^2} \right)^2}$$



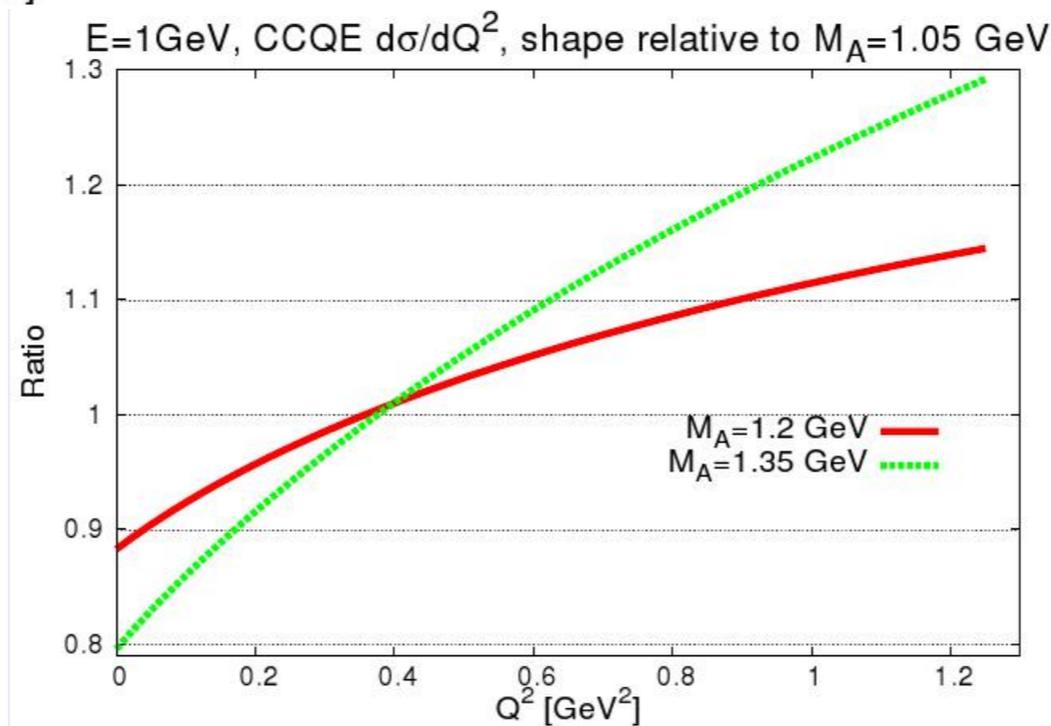
$$m = M_A$$

Q^2 dependence \Leftrightarrow Finite nucleon size

The Effect of M_A



Higher absolute cross section for higher M_A .



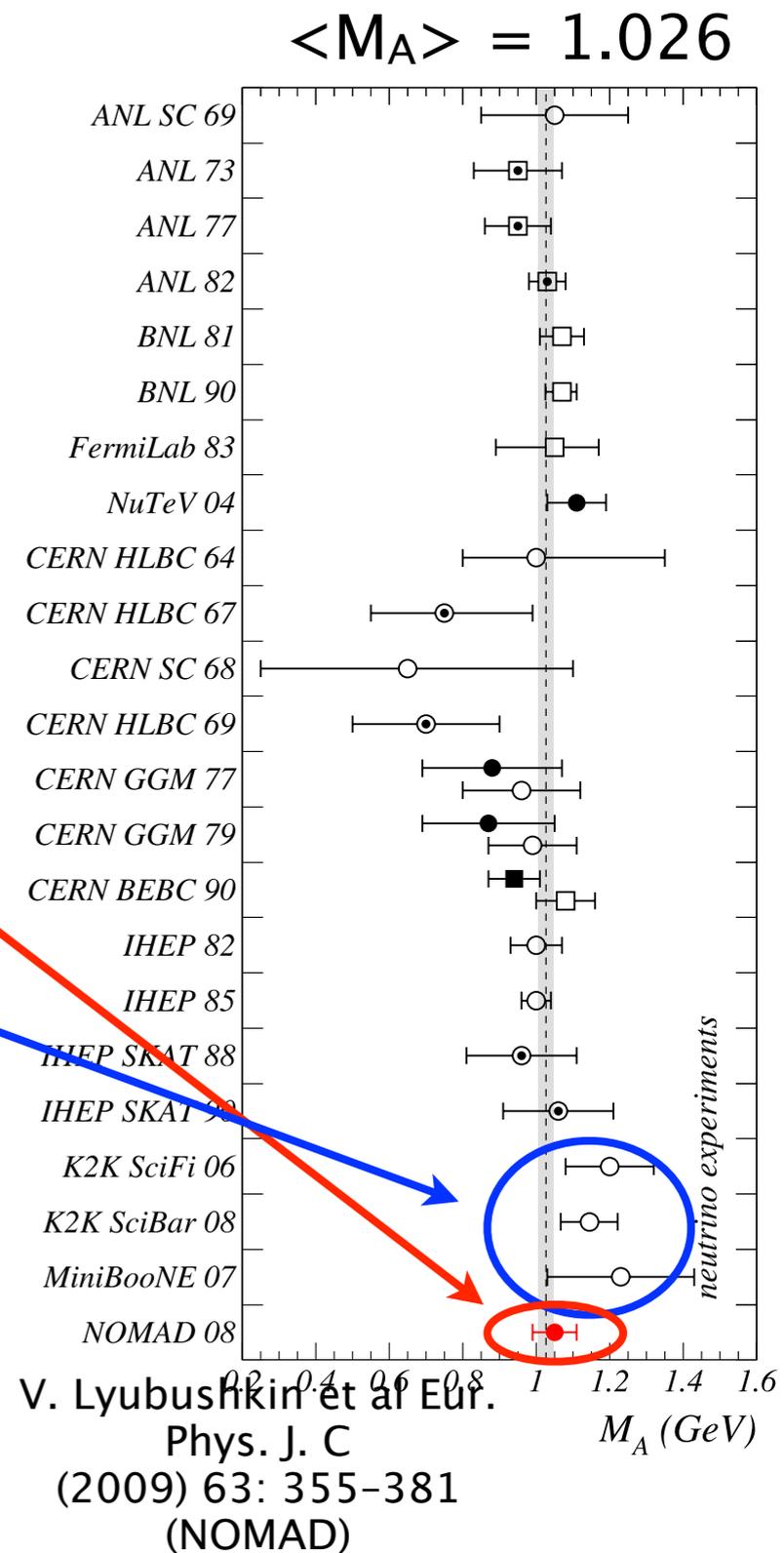
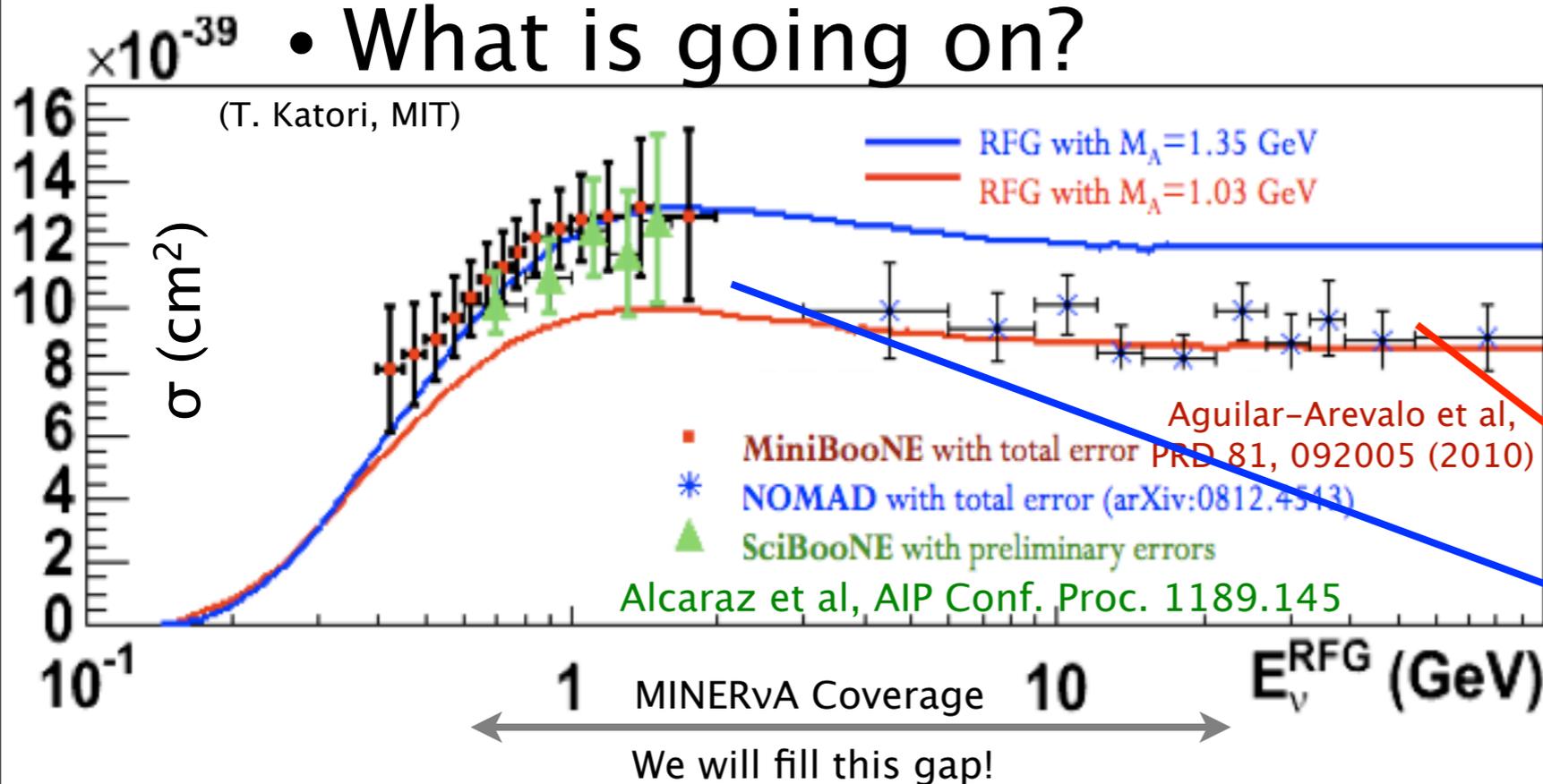
Relatively higher at high Q^2 for higher M_A .

Figures courtesy of J. Sobczyk

Is this picture of QE scatt. good enough ?

Modern experiments are high statistics measurements on heavy targets at low E.

• What is going on?



What is going on?



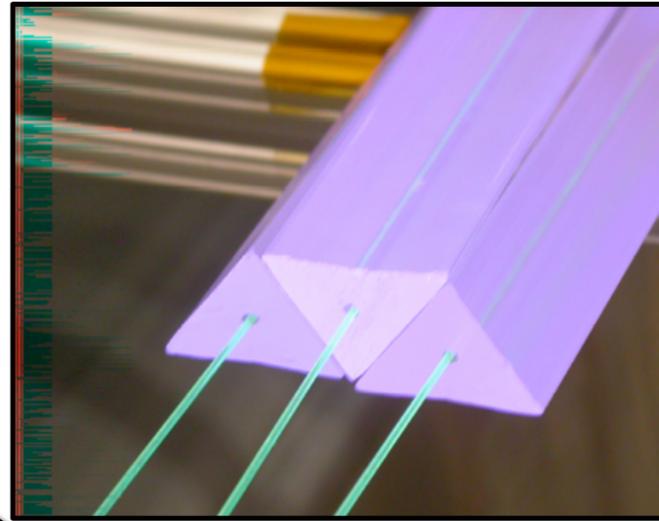
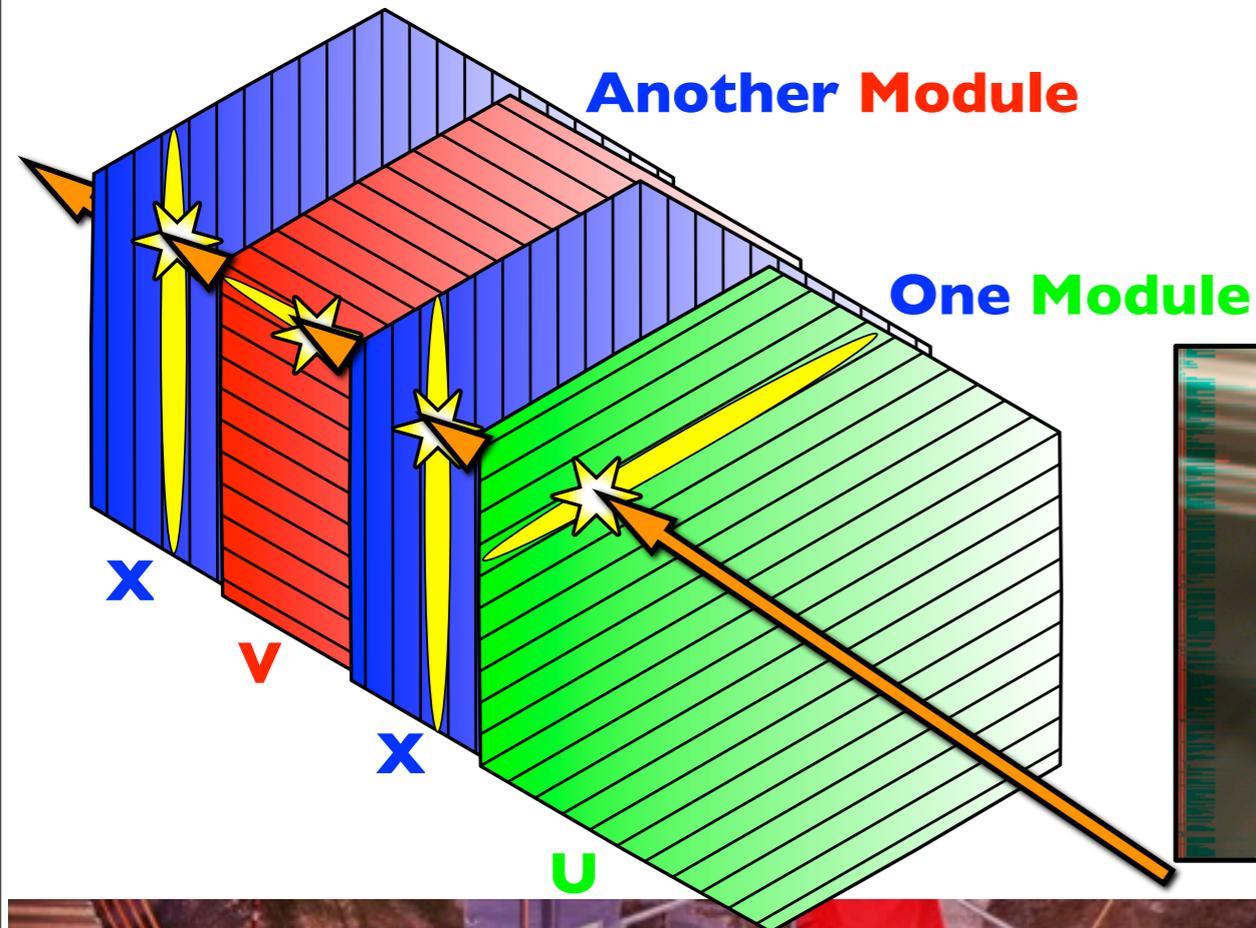
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MINERvA

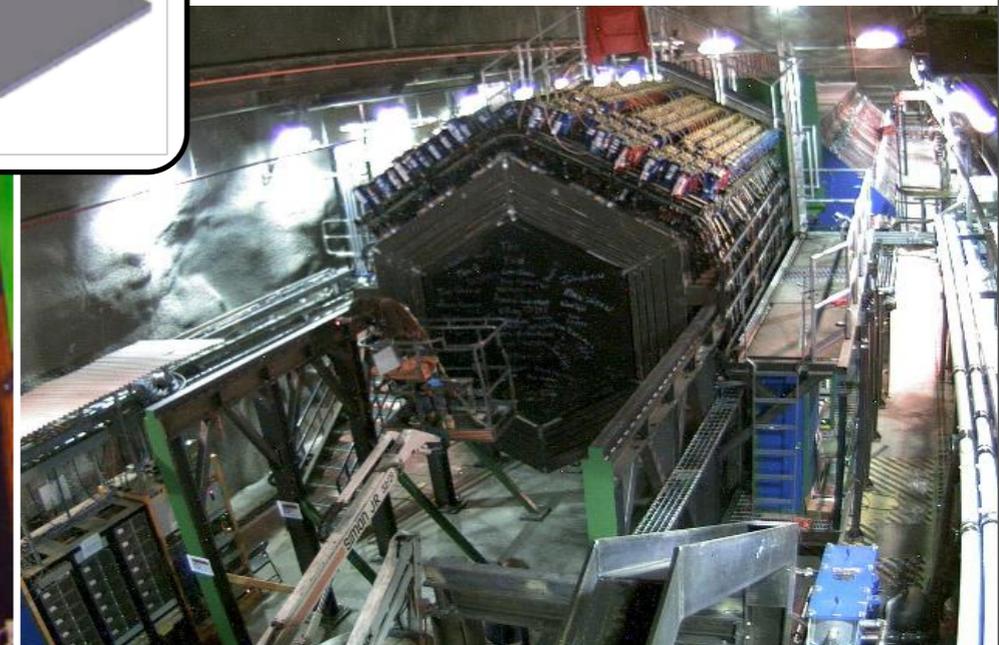
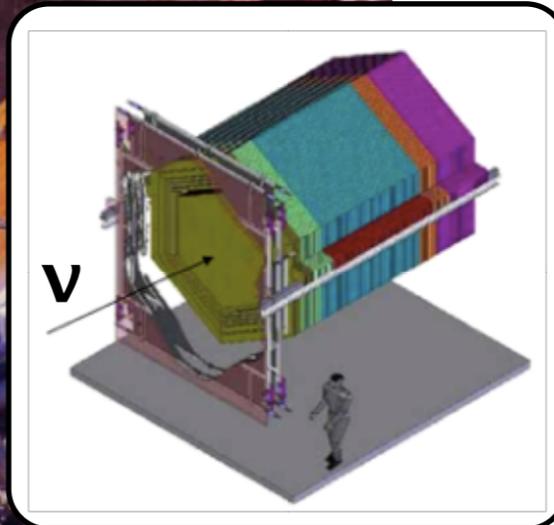
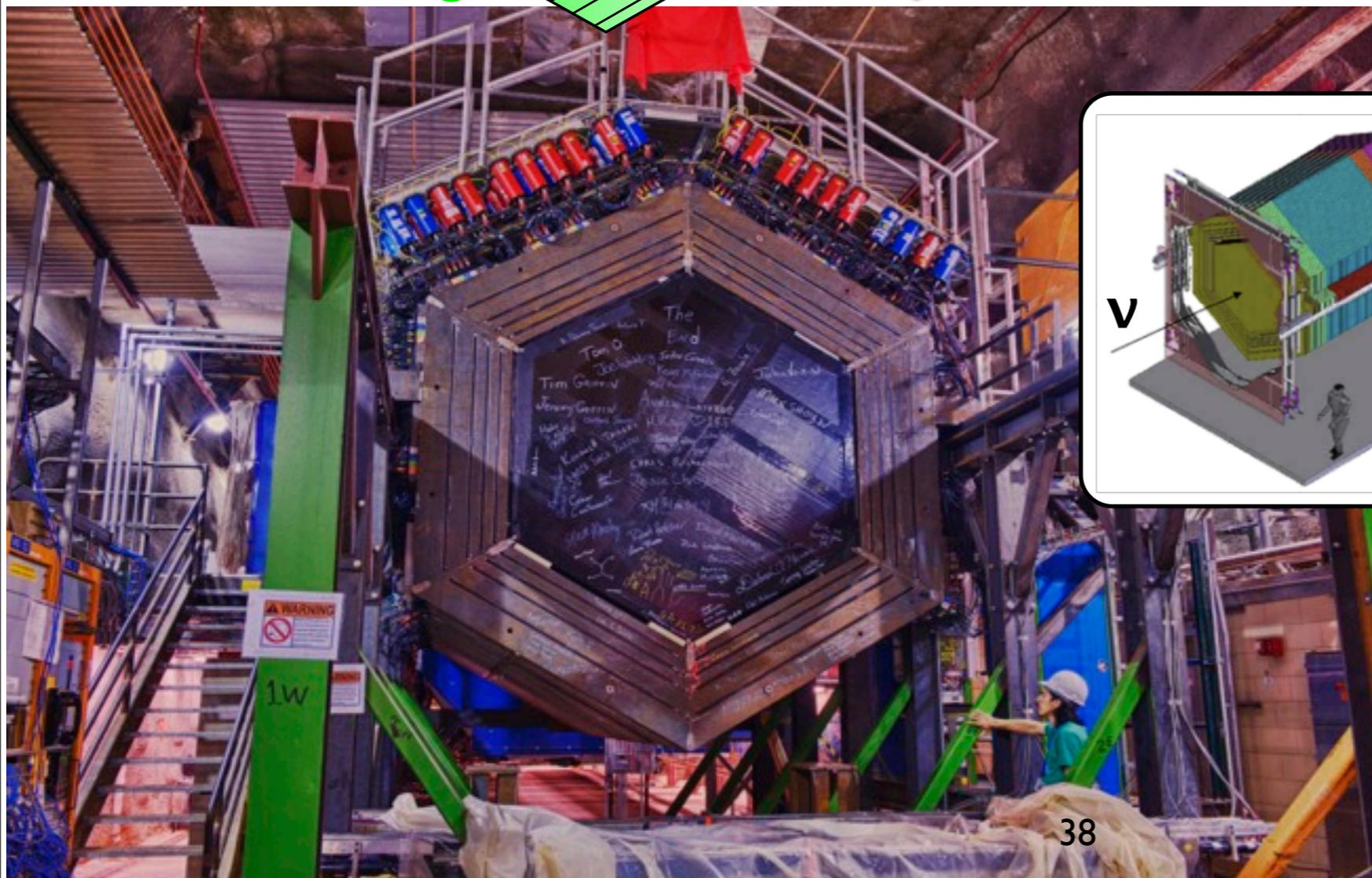


Another Module

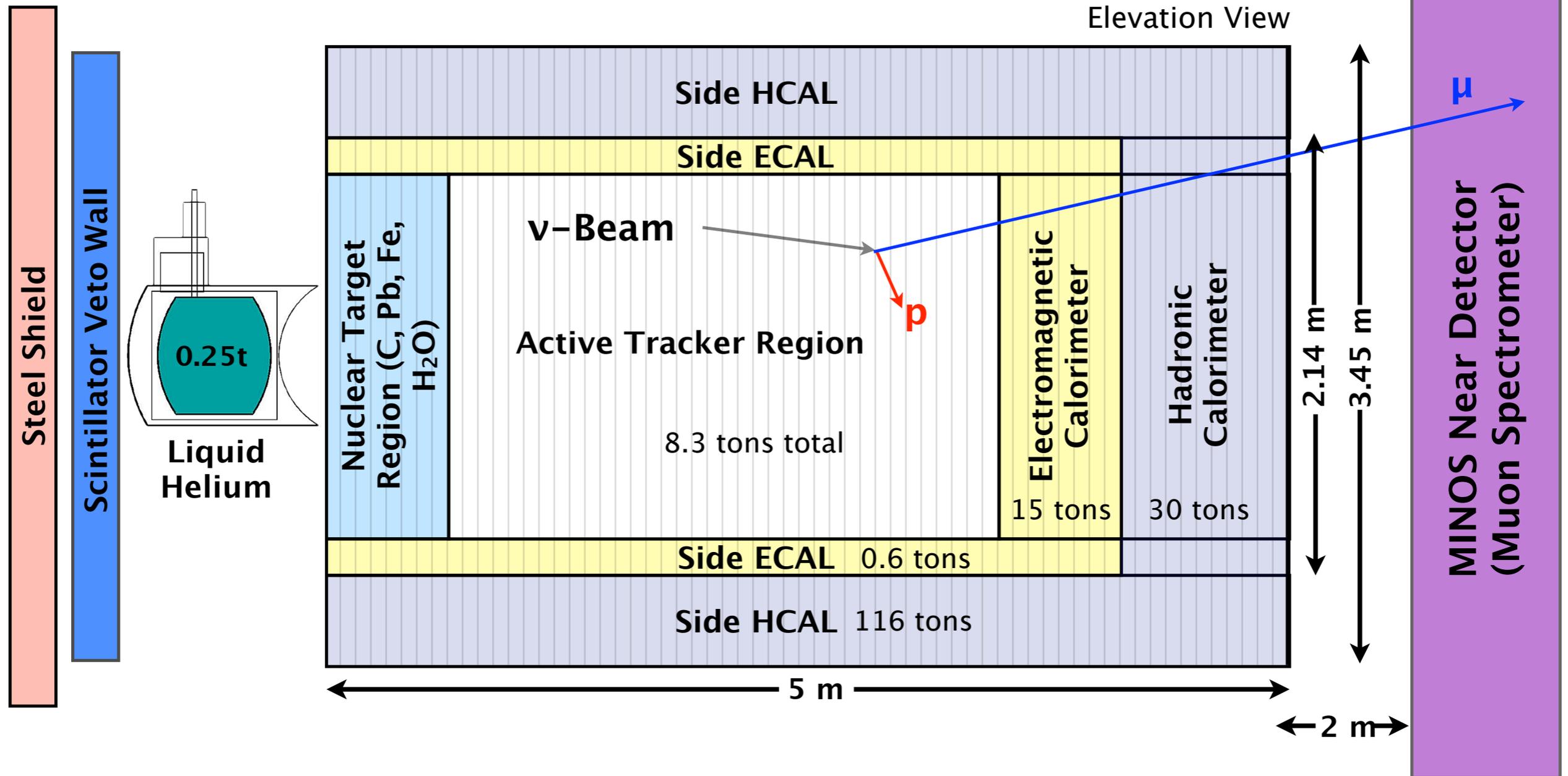
One Module



- Fine-grained resolution for excellent kinematic measurements.
- Low-energy cross-section program well-suited to next-generation oscillation experiments.
- Nuclear effects with a variety of target materials ranging from Helium to Lead. Especially important for ME run.



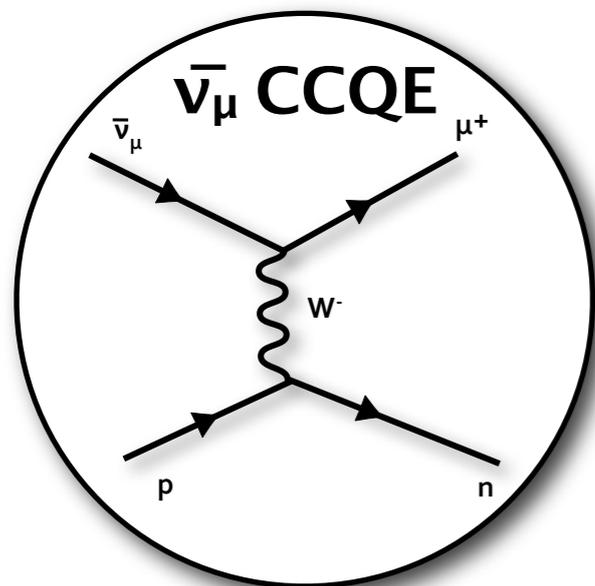
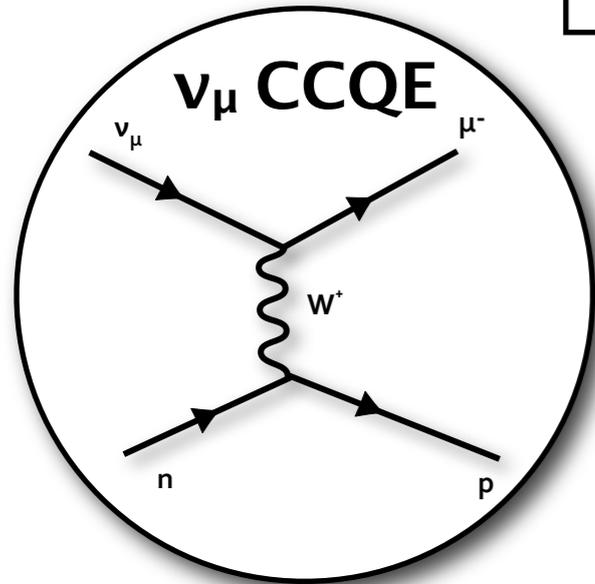
MINERvA - the detector design



- Detector composed of 120 stacked modules of varying composition.
- Finely segmented (~32 K readout channels), side ECAL & HCAL well instrumented
- MINOS near detector acts as magnetic spectrometer → muon charge and momentum

CCQE Physics Results

PRL 111, 022501 (2013) & PRL 111, 022502 (2013)

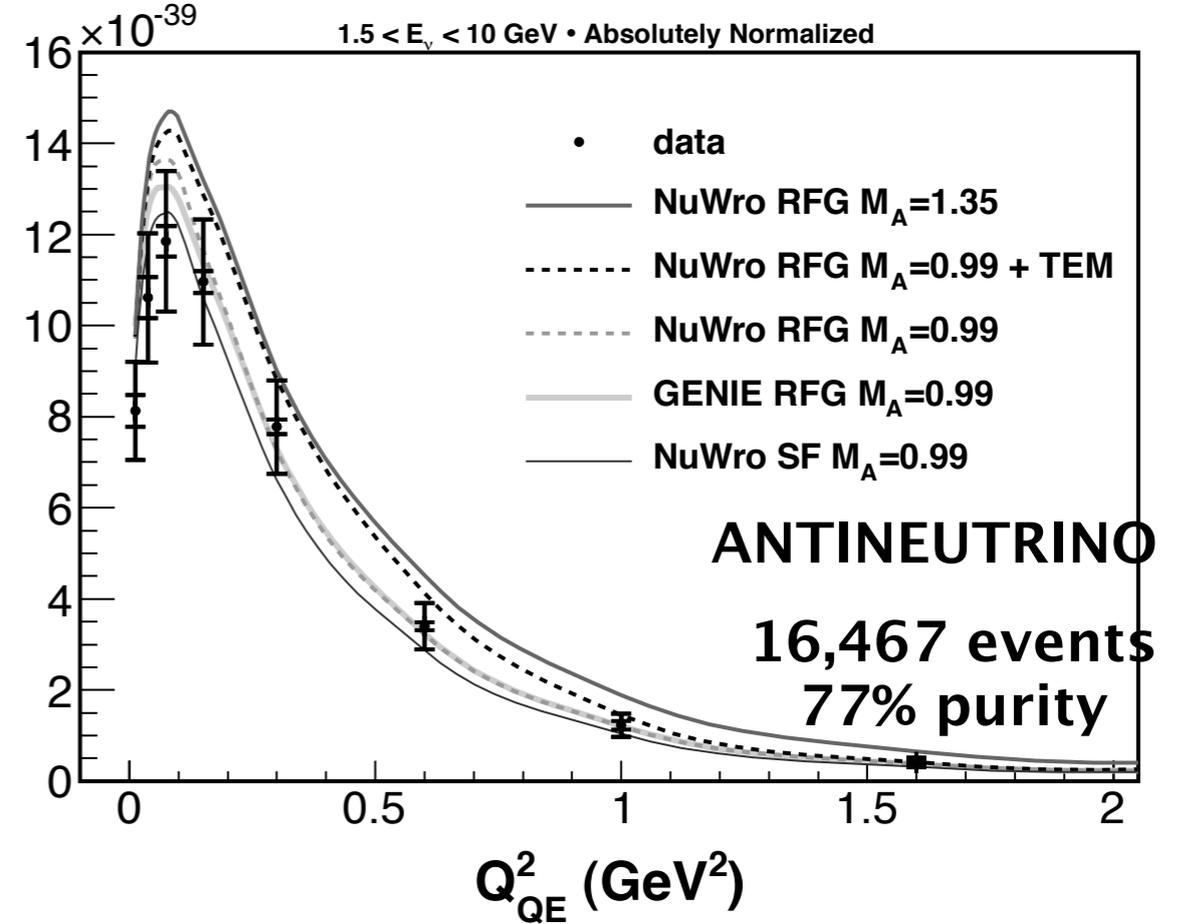
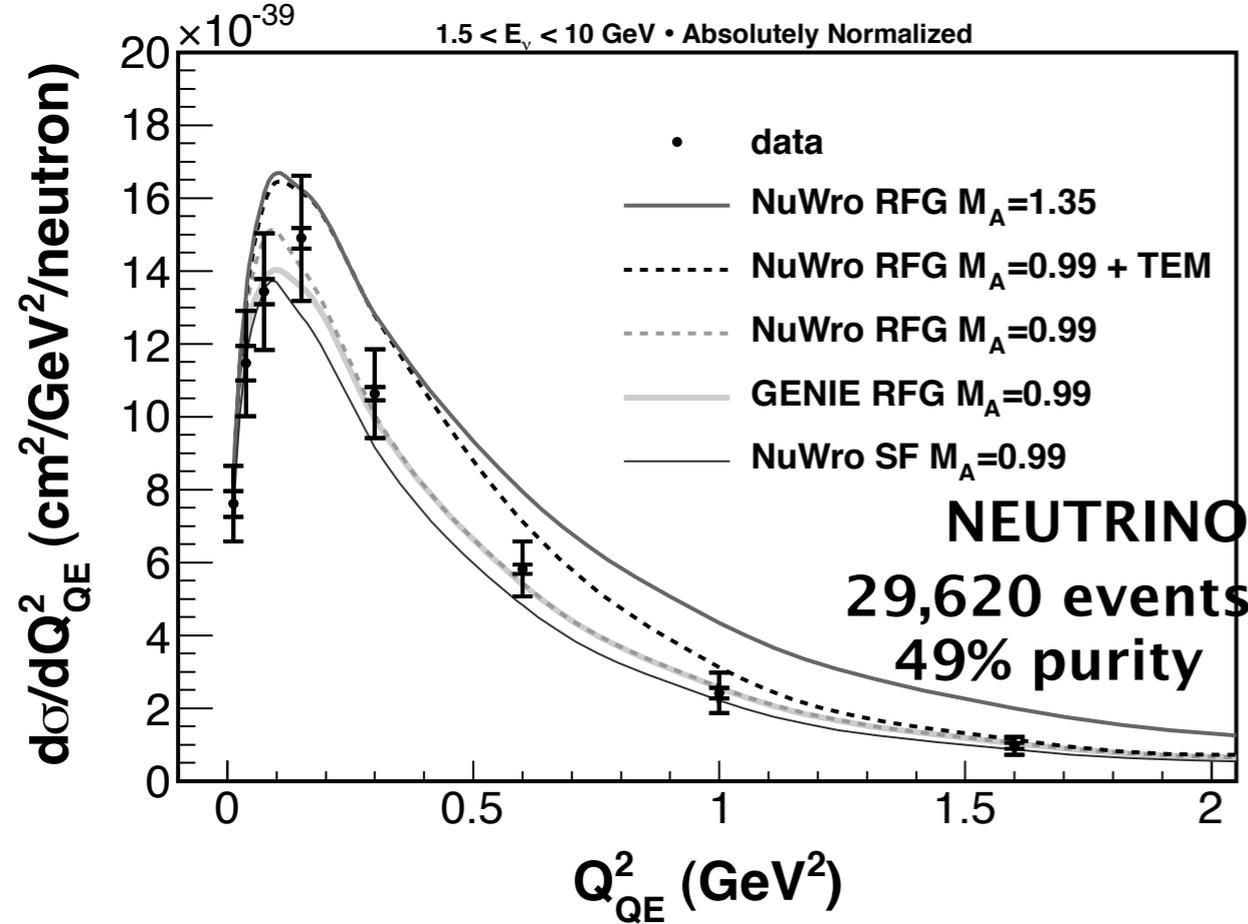


- $d\sigma/dQ^2$ on a (mostly) hydrocarbon target.
- Flux integrated over 1.5 to 10 GeV in the NuMI "Low Energy" Configuration.
- Muons are sign and momentum analyzed in the MINOS Near Detector (puts a lower-bound on momentum).
- See FNAL Wine & Cheese (D. Schmitz) on 10 May 2013 for more details.

$$Q_{QE}^2 = -m_{\mu}^2 + 2E_{\nu}^{QE} \left(E_{\mu} - \sqrt{E_{\mu}^2 - m_{\mu}^2} \cos \theta_{\mu} \right) = \text{Four momentum transfer}$$

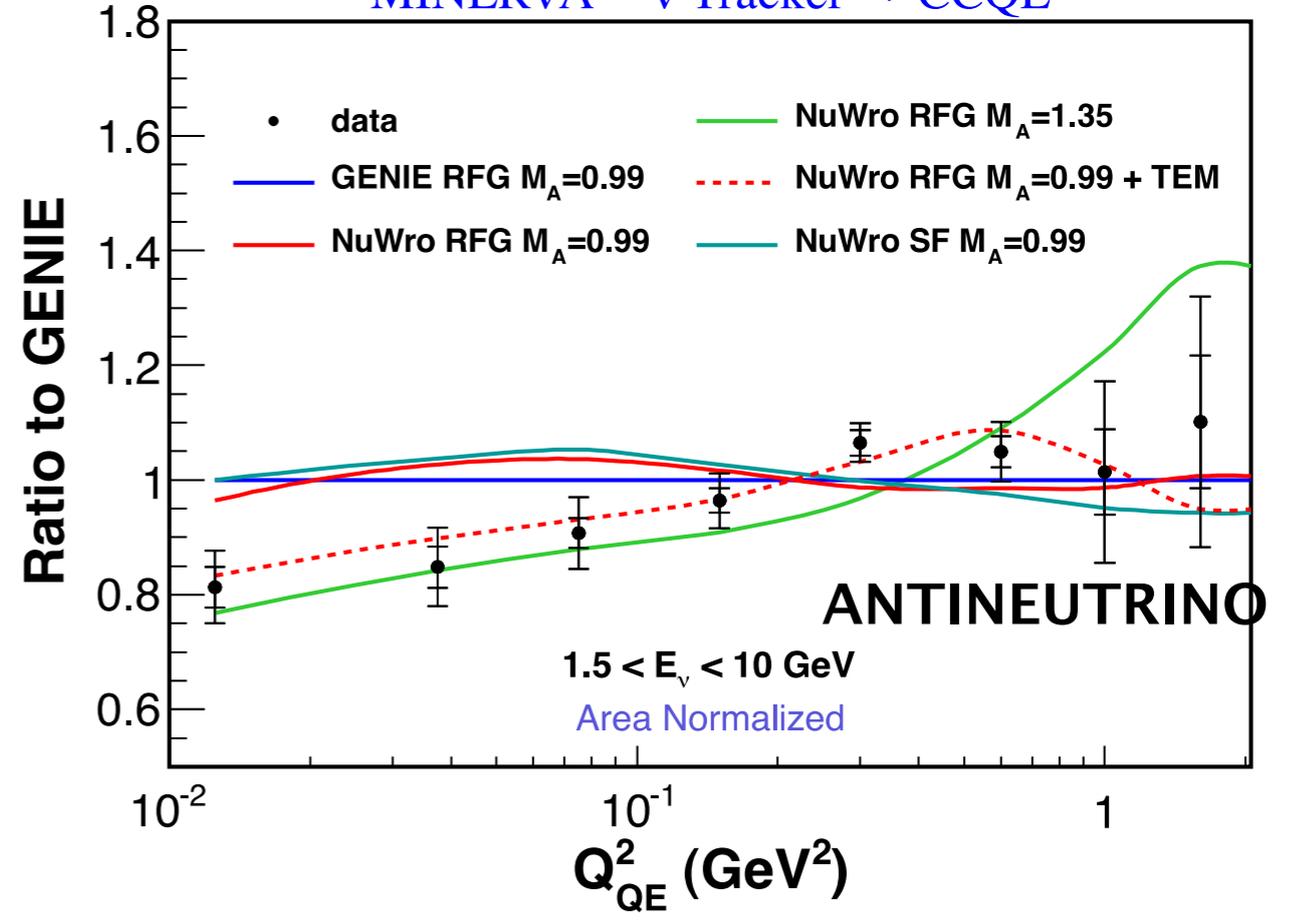
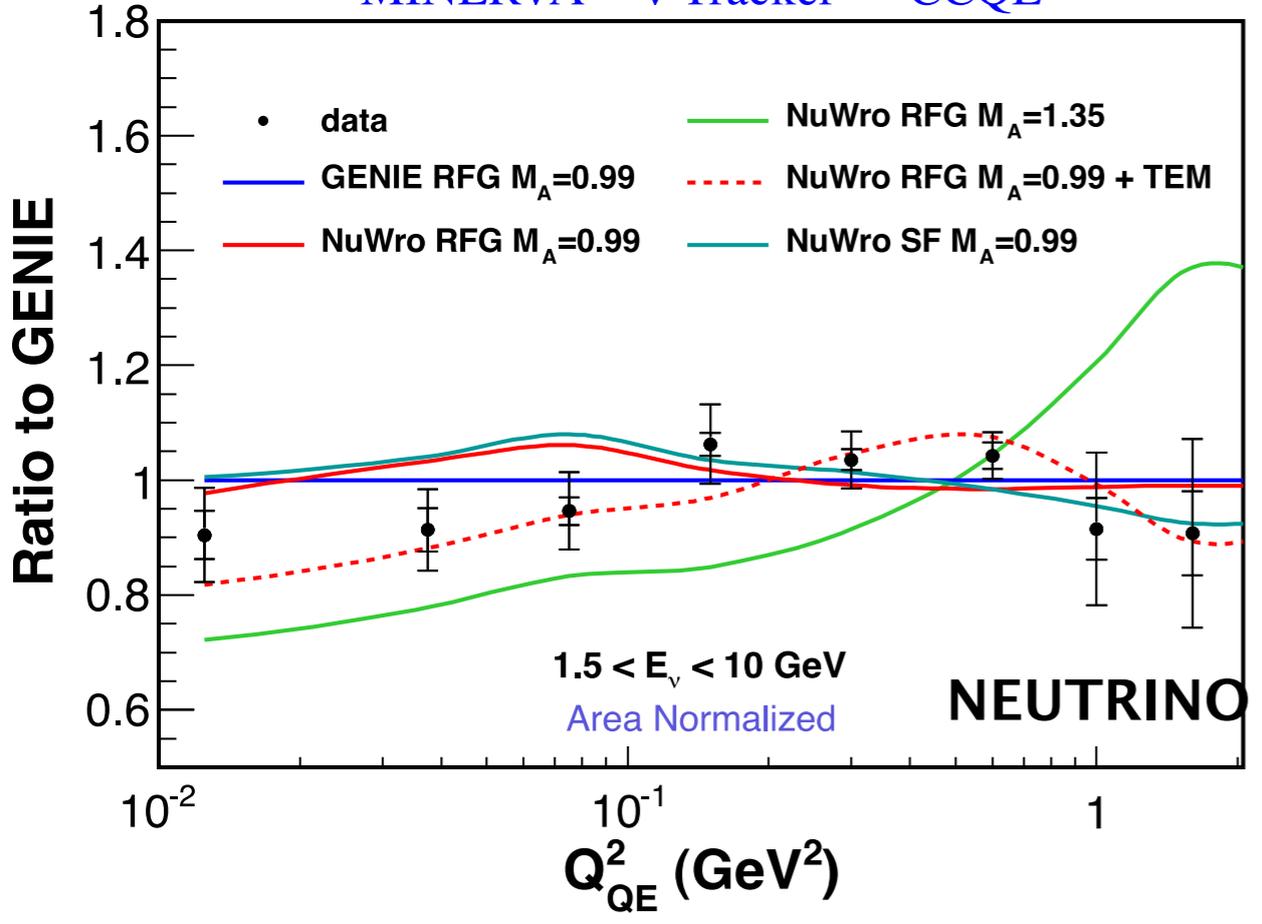
Nuclear Models

- **Relativistic Fermi Gas (RFG), $M_A = 0.99 \text{ GeV}/c^2$**
 - **The standard used in essentially all event generators.**
- **Relativistic Fermi Gas (RFG), $M_A = 1.35 \text{ GeV}/c^2$**
 - **Motivated by recent measurements & successful at low Q^2 .**
- **Nuclear Spectral Function (SF), $M_A = 0.99 \text{ GeV}/c^2$**
 - **A more realistic model of the nucleon momentum distribution.**
- **Transverse Enhancement Model (TEM), $M_A = 0.99 \text{ GeV}/c^2$**
 - **Empirical model modifying the magnetic form factors of bound nucleons to create the enhancement in the transverse cross-section observed in electron scattering (attributed to correlated pairs of nucleons).**
- **Vary one thing at a time in our comparisons...**



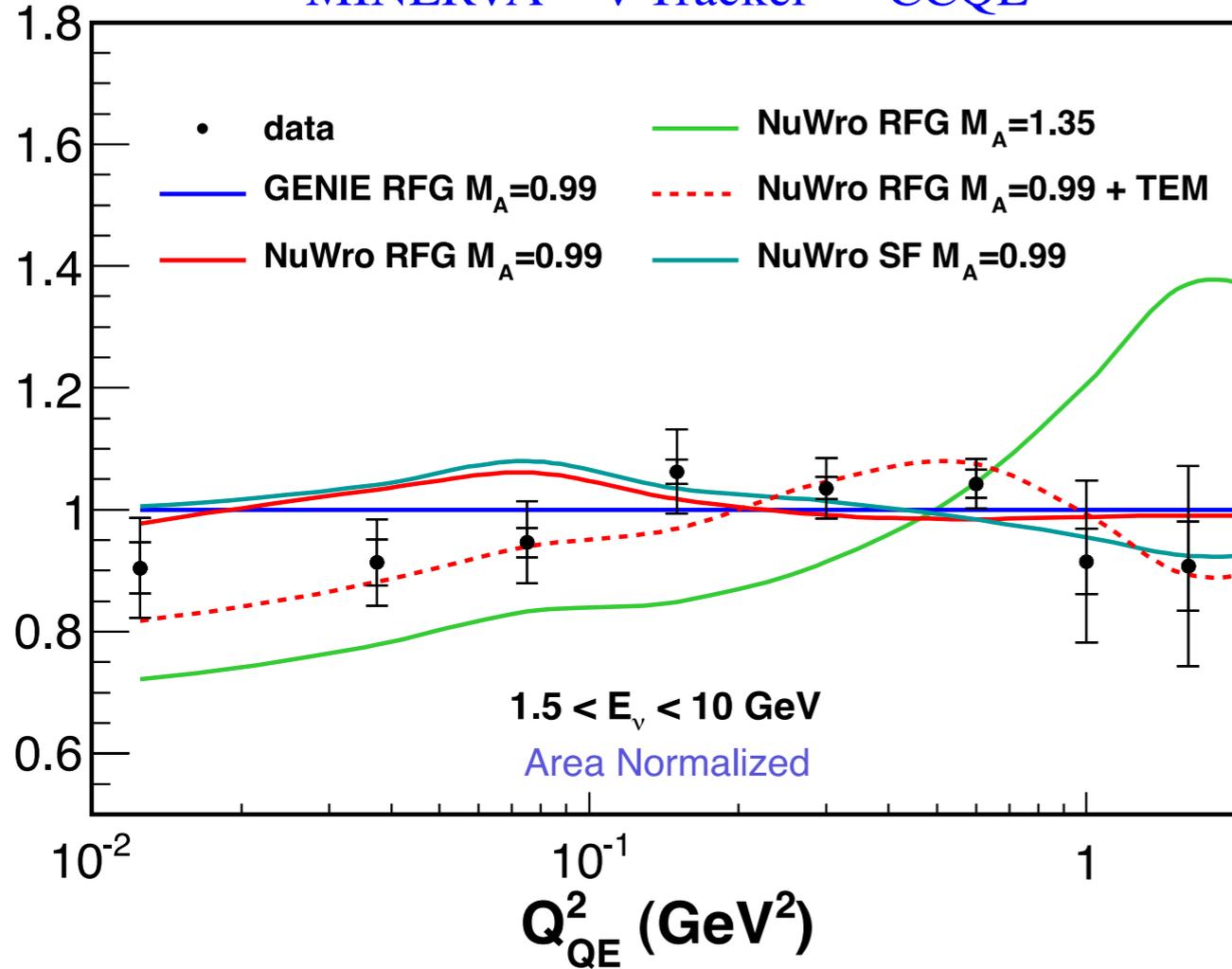
MINERvA • ν Tracker \rightarrow CCQE

MINERvA • $\bar{\nu}$ Tracker \rightarrow CCQE

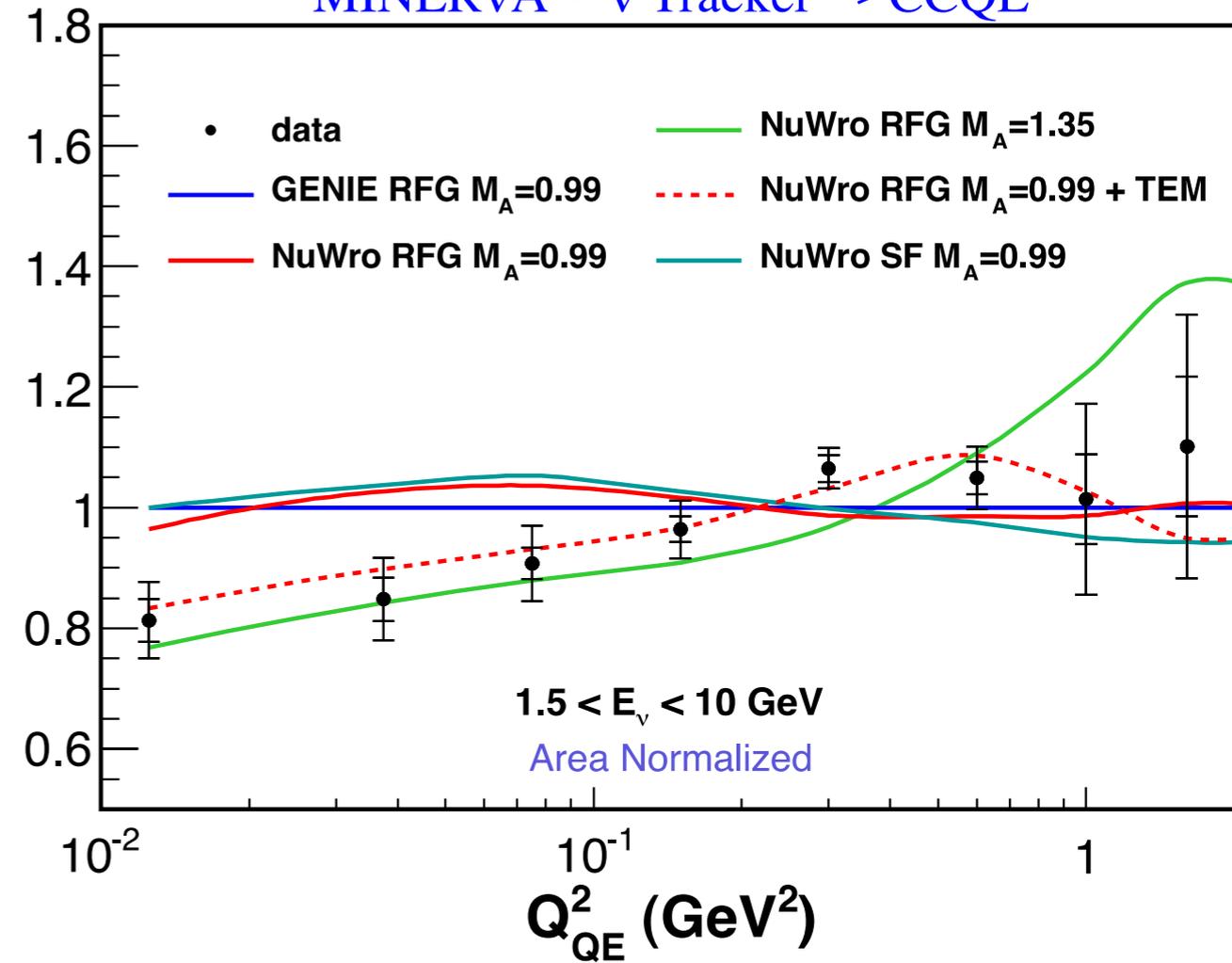


Neutrino (Left), Antineutrino (Right)

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Neutrino

NuWro Model	RFG	RFG +TEM	RFG	SF
M_A (GeV/ c^2)	0.99	0.99	1.35	0.99
Rate χ^2 /d.o.f.	3.5	2.4	3.7	2.8
Shape χ^2 /d.o.f.	4.1	1.7	2.1	3.8

Antineutrino

NuWro Model	RFG	RFG +TEM	RFG	SF
M_A (GeV)	0.99	0.99	1.35	0.99
Rate χ^2 /d.o.f.	2.64	1.06	2.90	2.14
Shape χ^2 /d.o.f.	2.90	0.66	1.73	2.99

A Recap of Discussions so far

- Neutrino-nucleon interactions are complex from a theoretical and experimental understanding point of view. Neutrino-nucleus gets even more difficult !
- Neutrino-electron and anti-neutrino-electron scattering cross-secs. have a factor of 3 difference. Backward ($\theta=0$) anti- ν_e scattering is forbidden due to helicity considerations !
- Neutrino-quark and anti-neutrino-quark scattering cross-secs. also have a factor of 3 difference. $\theta=\pi$ scattering is forbidden again !
- Neutrino Quasi-Elastic scattering is flagship signal channel in current and future generation neutrino oscillation experiments
- Neutrino energy and flavor inferred from just the lepton kinematics !
- However, it is not so simple - nuclear medium adds complexity
- Llewellyn Smith formalism uses simple model, assumes non-interacting nucleons, dipole form-factor, etc.
- MINERvA has published results on neutrino and anti-neutrino scattering on a mostly hydrocarbon target (PRL 111, 022501 (2013) and PRL 111, 022502 (2013) ! NuMI flux integrated over 1.5-10.0 GeV.
- Results presented in comparison to various nuclear models.

Lots of topics left uncovered today

- I gave hints of certain topics today, that need more time and slides for a better understanding of the physics involved in neutrino scattering, e.g. :
 - Free non-interacting nucleons inside the nucleus ?
 - Multi-nucleon ejection, short range correlations, etc. are some of the existing theories that attempt to model a more realistic picture of nucleons inside a nuclear medium.
 - Relativistic Fermi Gas model used in most current MC event generators
 - Ongoing work in theoretical field for improving nuclear models in event generators. Better models of final state interactions.
 - Flux is very crucial to neutrino cross-section measurements. Different methods adopted by different experiments at estimating their flux. Often multiple methods used for a better estimation.
 - Deep Inelastic Scattering, Resonance Processes
 - Complex topologies compared to QE scattering. Probe into affects like EMC, shadowing, anti-shadowing, etc. An exclusive talk will do justice to these topics.
- Please visit <http://minerva.fnal.gov/> - will answer a lot of the above questions

Other experimental results

- Unfortunately I could not cover results from other experiments today.....
 - MiniBooNE (<http://www-boone.fnal.gov/publications/>)
 - ArgoNeut (<http://t962.fnal.gov/Publications.html>)
 - MINOS (http://www-numi.fnal.gov/pr_plots/index.html)
 - SciBooNE (<http://www-sciboone.fnal.gov/documents/papers/papers.html>)
 - NOMAD (<http://www.nu.to.infn.it/exp/all/nomad/>)
 - LSND (<http://www.nu.to.infn.it/exp/all/lsnd>)
 - Expts. done at Jefferson Lab, SLAC - e.g. on Deep Inelastic Scattering
- Please visit the above websites for more information on neutrino scattering results

Thank you for your time !

Many thanks to all the slide & idea lenders for this talk !

Backup Slides